## **RF AND MICROWAVE TRANSMITTER DESIGN**

Andrei Grebennikov Bell Labs, Alcatel-Lucent, Ireland



### **RF AND MICROWAVE TRANSMITTER DESIGN**

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## CONTENTS

Pro	eface		xiii	
Int	trodu	ction	1	
	Refe	rences 6		
1	Passive Elements and Circuit Theory			
	1.1 1.2 1.3 1.4	Immittance Two-Port Network Parameters9Scattering Parameters13Interconnections of Two-Port Networks17Practical Two-Port Networks201.4.1Single-Element Networks201.4.2 $\pi$ - and $T$ -Type Networks21		
	1.5 1.6	Three-Port Network with Common Terminal 24		
	1.0	1.6.1     Inductors     26       1.6.2     Capacitors     29		
<ol> <li>1.7 Transmission Line 31</li> <li>1.8 Types of Transmission Lines 35</li> </ol>		Transmission Line 31 Types of Transmission Lines 35		
		<ul> <li>1.8.1 Coaxial Line 35</li> <li>1.8.2 Stripline 36</li> <li>1.8.3 Microstrip Line 39</li> <li>1.8.4 Slotline 41</li> <li>1.8.5 Coplanar Waveguide 42</li> </ul>		
	1.9	Noise 44		
		1.9.1Noise Sources441.9.2Noise Figure461.9.3Flicker Noise53		
	Refe	rences 53		
2	Acti	ve Devices and Modeling	57	
	2.1	Diodes 57 2.1.1 Operation Principle 57 2.1.2 Schottky Diodes 59 2.1.3 $p-i-n$ Diodes 61		
	2.2	2.1.4 Zener Diodes 62		
	2.2	varactors     03       2.2.1     Varactor Modeling       63     2.2.2       MOS     Varactor       65		

- 2.3 MOSFETs 70
  - 2.3.1 Small-Signal Equivalent Circuit 70
  - 2.3.2 Nonlinear I–V Models 73
  - 2.3.3 Nonlinear C–V Models 75
  - 2.3.4 Charge Conservation 78
  - 2.3.5 Gate–Source Resistance 79
  - 2.3.6 Temperature Dependence 79
  - 2.3.7 Noise Model 81
- 2.4 MESFETs and HEMTs 83
  - 2.4.1 Small-Signal Equivalent Circuit 83
  - 2.4.2 Determination of Equivalent Circuit Elements 85
  - 2.4.3 Curtice Quadratic Nonlinear Model 88
  - 2.4.4 Parker–Skellern Nonlinear Model 89
  - 2.4.5 Chalmers (Angelov) Nonlinear Model 91
  - 2.4.6 IAF (Berroth) Nonlinear Model 93
  - 2.4.7 Noise Model 94
- 2.5 BJTs and HBTs 97
  - 2.5.1 Small-Signal Equivalent Circuit 97
  - 2.5.2 Determination of Equivalent Circuit Elements 98
  - 2.5.3 Equivalence of Intrinsic  $\pi$  and T-Type Topologies 100
  - 2.5.4 Nonlinear Bipolar Device Modeling 102
  - 2.5.5 Noise Model 105

References 107

#### **3** Impedance Matching

- 3.1 Main Principles 113
- 3.2 Smith Chart 116
- 3.3 Matching with Lumped Elements 120
  - 3.3.1 Analytic Design Technique 120
  - 3.3.2 Bipolar UHF Power Amplifier 131
  - 3.3.3 MOSFET VHF High-Power Amplifier 135
- 3.4 Matching with Transmission Lines 138
  - 3.4.1 Analytic Design Technique 138
  - 3.4.2 Equivalence Between Circuits with Lumped and Distributed Parameters 144
  - 3.4.3 Narrowband Microwave Power Amplifier 147
  - 3.4.4 Broadband UHF High-Power Amplifier 149

3.5 Matching Networks with Mixed Lumped and Distributed Elements 151 References 153

#### 4 Power Transformers, Combiners, and Couplers

- 4.1 Basic Properties 155
  - 4.1.1 Three-Port Networks 155
  - 4.1.2 Four-Port Networks 156
- 4.2 Transmission-Line Transformers and Combiners 158

#### 113

4.3 Baluns 168
4.4 Wilkinson Power Dividers/Combiners 174
4.5 Microwave Hybrids 182
4.6 Coupled-Line Directional Couplers 192
References 197

#### 5 Filters

- 5.1 Types of Filters 201
- 5.2 Filter Design Using Image Parameter Method 205
  - 5.2.1 Constant-*k* Filter Sections 205
  - 5.2.2 *m*-Derived Filter Sections 207
- 5.3 Filter Design Using Insertion Loss Method 210
  - 5.3.1 Maximally Flat Low-Pass Filter 210
  - 5.3.2 Equal-Ripple Low-Pass Filter 213
  - 5.3.3 Elliptic Function Low-Pass Filter 216
  - 5.3.4 Maximally Flat Group-Delay Low-Pass Filter 219
- 5.4 Bandpass and Bandstop Transformation 222
- 5.5 Transmission-Line Low-Pass Filter Implementation 225
  - 5.5.1 Richards's Transformation 225
  - 5.5.2 Kuroda Identities 226
  - 5.5.3 Design Example 228
- 5.6 Coupled-Line Filters 228
  - 5.6.1 Impedance and Admittance Inverters 228
  - 5.6.2 Coupled-Line Section 231
  - 5.6.3 Parallel-Coupled Bandpass Filters Using Half-Wavelength Resonators 234
  - 5.6.4 Interdigital, Combline, and Hairpin Bandpass Filters 236
  - 5.6.5 Microstrip Filters with Unequal Phase Velocities 239
  - 5.6.6 Bandpass and Bandstop Filters Using Quarter-Wavelength Resonators 241
- 5.7 SAW and BAW Filters 243

References 250

#### 6 Modulation and Modulators

- 6.1 Amplitude Modulation 255
  - 6.1.1 Basic Principle 255
  - 6.1.2 Amplitude Modulators 259
- 6.2 Single-Sideband Modulation 262
  - 6.2.1 Double-Sideband Modulation 262
  - 6.2.2 Single-Sideband Generation 265
  - 6.2.3 Single-Sideband Modulator 266
- 6.3 Frequency Modulation 267
  - 6.3.1 Basic Principle 268
  - 6.3.2 Frequency Modulators 273
- 6.4 Phase Modulation 278

- 6.5 Digital Modulation 283
  - 6.5.1 Amplitude Shift Keying 284
  - 6.5.2 Frequency Shift Keying 287
  - 6.5.3 Phase Shift Keying 289
  - 6.5.4 Minimum Shift Keying 296
  - 6.5.5 Quadrature Amplitude Modulation 299
  - 6.5.6 Pulse Code Modulation 300
- 6.6 Class-S Modulator 302
- 6.7 Multiple Access Techniques 304
  - 6.7.1 Time and Frequency Division Multiplexing 304
  - 6.7.2 Frequency Division Multiple Access 305
  - 6.7.3 Time Division Multiple Access 305
  - 6.7.4 Code Division Multiple Access 306

References 308

#### 7 Mixers and Multipliers

- 7.1 Basic Theory 311
- 7.2 Single-Diode Mixers 313
- 7.3 Balanced Diode Mixers 318
  - 7.3.1 Single-Balanced Mixers 318
  - 7.3.2 Double-Balanced Mixers 321
- 7.4 Transistor Mixers 326
- 7.5 Dual-Gate FET Mixer 329
- 7.6 Balanced Transistor Mixers 331
  - 7.6.1 Single-Balanced Mixers 331
  - 7.6.2 Double-Balanced Mixers 334
- 7.7 Frequency Multipliers 338
- References 344

#### 8 Oscillators

- 8.1 Oscillator Operation Principles 347
  - 8.1.1 Steady-State Operation Mode 347
  - 8.1.2 Start-Up Conditions 349
- 8.2 Oscillator Configurations and Historical Aspect 353
- 8.3 Self-Bias Condition 358
- 8.4 Parallel Feedback Oscillator 362
- 8.5 Series Feedback Oscillator 365
- 8.6 Push–Push Oscillators 368
- 8.7 Stability of Self-Oscillations 372
- 8.8 Optimum Design Techniques 3768.8.1 Empirical Approach 3768.8.2 Analytic Approach 379
- 8.9 Noise in Oscillators 385
  - 8.9.1 Parallel Feedback Oscillator 386

347

- 8.9.2 Negative Resistance Oscillator 392
- 8.9.3 Colpitts Oscillator 394
- 8.9.4 Impulse Response Model 397
- 8.10 Voltage-Controlled Oscillators 407
- 8.11 Crystal Oscillators 417
- 8.12 Dielectric Resonator Oscillators 423

References 428

#### 9 Phase-Locked Loops

- 9.1 Basic Loop Structure 433
- 9.2 Analog Phase-Locked Loops 435
- 9.3 Charge-Pump Phase-Locked Loops 439
- 9.4 Digital Phase-Locked Loops 441
- 9.5 Loop Components 444
  - 9.5.1 Phase Detector 444
  - 9.5.2 Loop Filter 449
  - 9.5.3 Frequency Divider 454
  - 9.5.4 Voltage-Controlled Oscillator 457
- 9.6 Loop Parameters 461
  - 9.6.1 Lock Range 461
  - 9.6.2 Stability 462
  - 9.6.3 Transient Response 463
  - 9.6.4 Noise 465
- 9.7 Phase Modulation Using Phase-Locked Loops 466
- 9.8 Frequency Synthesizers 469
  - 9.8.1 Direct Analog Synthesizers 469
  - 9.8.2 Integer-N Synthesizers Using PLL 469
  - 9.8.3 Fractional-N Synthesizers Using PLL 471
  - 9.8.4 Direct Digital Synthesizers 473

References 474

#### 10 Power Amplifier Design Fundamentals

- 10.1 Power Gain and Stability 477
- 10.2 Basic Classes of Operation: A, AB, B, and C 487
- 10.3 Linearity 496
- 10.4 Nonlinear Effect of Collector Capacitance 503
- 10.5 DC Biasing 506
- 10.6 Push–Pull Power Amplifiers 515
- 10.7 Broadband Power Amplifiers 522
- 10.8 Distributed Power Amplifiers 537
- 10.9 Harmonic Tuning Using Load–Pull Techniques 543
- 10.10 Thermal Characteristics 549

References 552

#### x CONTENTS

#### 11 High-Efficiency Power Amplifiers

- 11.1 Class D 557
  - 11.1.1 Voltage-Switching Configurations 557
  - 11.1.2 Current-Switching Configurations 561
  - 11.1.3 Drive and Transition Time 564
- 11.2 Class F 567
  - 11.2.1 Idealized Class F Mode 569
  - 11.2.2 Class F with Quarterwave Transmission Line 572
  - 11.2.3 Effect of Saturation Resistance 575
  - 11.2.4 Load Networks with Lumped and Distributed Parameters 577
- 11.3 Inverse Class F 581
  - 11.3.1 Idealized Inverse Class F Mode 583
  - 11.3.2 Inverse Class F with Quarterwave Transmission Line 585
  - 11.3.3 Load Networks with Lumped and Distributed Parameters 586
- 11.4 Class E with Shunt Capacitance 589
  - 11.4.1 Optimum Load Network Parameters 590
  - 11.4.2 Saturation Resistance and Switching Time 595
  - 11.4.3 Load Network with Transmission Lines 599
- 11.5 Class E with Finite dc-Feed Inductance 601
  - 11.5.1 General Analysis and Optimum Circuit Parameters 601
  - 11.5.2 Parallel-Circuit Class E 605
  - 11.5.3 Broadband Class E 610
  - 11.5.4 Power Gain 613
- 11.6 Class E with Quarterwave Transmission Line 615
  - 11.6.1 General Analysis and Optimum Circuit Parameters 615
  - 11.6.2 Load Network with Zero Series Reactance 622
  - 11.6.3 Matching Circuits with Lumped and Distributed Parameters 625
- 11.7 Class FE 628
- 11.8 CAD Design Example: 1.75 GHz HBT Class E MMIC Power Amplifier 638

References 653

#### 12 Linearization and Efficiency Enhancement Techniques

657

- 12.1 Feedforward Amplifier Architecture 657
- 12.2 Cross Cancellation Technique 663
- 12.3 Reflect Forward Linearization Amplifier 665
- 12.4 Predistortion Linearization 666
- 12.5 Feedback Linearization 672
- 12.6 Doherty Power Amplifier Architectures 678
- 12.7 Outphasing Power Amplifiers 685
- 12.8 Envelope Tracking 691
- 12.9 Switched Multipath Power Amplifiers 695
- 12.10 Kahn EER Technique and Digital Power Amplification 702
  - 12.10.1 Envelope Elimination and Restoration 702
  - 12.10.2 Pulse-Width Carrier Modulation 704

717

759

	12.10.3 Class S Amplifier 706 12.10.4 Digital RF Amplification	706			
References 709					
13	Control Circuits				

- 13.1 Power Detector and VSWR Protection 717
- 13.2 Switches 722
- 13.3 Phase Shifters 728
  - 13.3.1 Diode Phase Shifters 729
  - 13.3.2 Schiffman 90° Phase Shifter 736
  - 13.3.3 MESFET Phase Shifters 739
- 13.4 Attenuators 741
- 13.5 Variable Gain Amplifiers 746
- 13.6 Limiters 750

References 753

#### 14 Transmitter Architectures

- 14.1 Amplitude-Modulated Transmitters 759
  - 14.1.1 Collector Modulation 760
  - 14.1.2 Base Modulation 762
  - 14.1.3 Low-Level Modulation 764
  - 14.1.4 Amplitude Keying 765
- 14.2 Single-Sideband Transmitters 766
- 14.3 Frequency-Modulated Transmitters 768
- 14.4 Television Transmitters 772
- 14.5 Wireless Communication Transmitters 776
- 14.6 Radar Transmitters 782
  - 14.6.1 Phased-Array Radars 783
  - 14.6.2 Automotive Radars 786
  - 14.6.3 Electronic Warfare 791
- 14.7 Satellite Transmitters 794
- 14.8 Ultra-Wideband Communication Transmitters 797

References 802

#### Index

### PREFACE

The main objective of this book is to present all relevant information required to design the transmitters in general and their main components in particular in different RF and microwave applications including well-known historical and recent novel architectures, theoretical approaches, circuit simulation results, and practical implementation techniques. This comprehensive book can be very useful for lecturing to promote the systematic way of thinking with analytical calculations and practical verification, thus making a bridge between theory and practice of RF and microwave engineering. As a result, this book is intended for and can be recommended to *university-level professors* as a comprehensive material to help in lecturing for graduate and postgraduate students, to *researchers and scientists* to combine the theoretical analysis with practical design and to provide a sufficient basis for innovative ideas and circuit design techniques, and to *practicing designers and engineers* as the book contains numerous well-known and novel practical circuits, architectures, and theoretical approaches with detailed description of their operational principles and applications.

Chapter 1 introduces the basic two-port networks describing the behavior of linear and nonlinear circuits. To characterize the nonlinear properties of the bipolar or field-effect transistors, their equivalent circuit elements are expressed through the impedance *Z*-parameters, admittance *Y*-parameters, or hybrid *H*-parameters. On the other hand, the transmission *ABCD*-parameters are very important for the design of the distributed circuits such as a transmission line or cascaded elements, whereas the scattering *S*-parameters are widely used to simplify the measurement procedure. The design formulas and curves are given for several types of transmission lines including stripline, microstrip line, slotline, and coplanar waveguide. Monolithic implementation of lumped inductors and capacitors is usually required at microwave frequencies and for portable devices. Knowledge of noise phenomena such as noise figure, additive white noise, low-frequency fluctuations, or flicker noise in active or passive elements is very important for the oscillator modeling in particular and entire transmitter design in general.

In Chapter 2, all necessary steps to provide an accurate device modeling procedure starting with the determination of the device small-signal equivalent circuit parameters are described and discussed. A variety of nonlinear models for MOSFET, MESFET, HEMT, and BJT devices including HBTs, which are very prospective for modern microwave monolithic integrated circuits, are given. In order to highlight the advantages or drawbacks of one over another nonlinear device model, a comparison of the measured and modeled volt–ampere and voltage–capacitance characteristics, as well as a frequency range of model application, are analyzed.

The main principles and impedance matching tools are described in Chapter 3. Generally, an optimum solution depends on the circuit requirements, such as the simplicity in practical realization, frequency bandwidth and minimum power ripple, design implementation and adjustability, stable operation conditions, and sufficient harmonic suppression. As a result, many types of the matching networks are available, including lumped elements and transmission lines. To simplify and visualize the matching design procedure, an analytical approach, which allows calculation of the parameters of the matching circuits using simple equations, and Smith chart traces are discussed. In addition, several examples of the narrowband and broadband power amplifiers using bipolar or MOSFET devices are given, including successive and detailed design considerations and explanations.

Chapter 4 describes the basic properties of the three-port and four-port networks, as well as a variety of different combiners, transformers, and directional couplers for RF and microwave power

applications. For power combining in view of insufficient power performance of the active devices, it is best to use the coaxial-cable combiners with ferrite core to combine the output powers of RF power amplifiers intended for wideband applications. Since the device output impedance is usually too small for high power level, to match this impedance with a standard 50- $\Omega$  load, it is necessary to use the coaxial-line transformers with specified impedance transformation. For narrowband applications, the *N*-way Wilkinson combiners are widely used due to the simplicity of their practical realization. At the same time, the size of the combiners should be very small at microwave frequencies. Therefore, the commonly used hybrid microstrip combiners including different types of the microwave hybrids and directional couplers are described and analyzed.

Chapter 5 introduces the basic types of RF and microwave filters based on the low-pass or highpass sections and bandpass or bandstop transformation. Classical filter design approaches using image parameter and insertion loss methods are given for low-pass and high-pass *LC* filter implementations. The quarterwave-line and coupled-line sections, which are the basic elements of microwave transmission-line filters, are described and analyzed. Different examples of coupled-line filters including interdigital, combline, and hairpin bandpass filters are given. Special attention is paid to microstrip filters with unequal phase velocities, which can provide unexpected properties because of different implementation technologies. Finally, the typical structures, implementation technology, operational principles, and band performance of the filters based on surface and bulk acoustic waves are presented.

Chapter 6 discusses the basic features of different types of analog modulation including amplitude, single-sideband, frequency, and phase modulation, and basic types of digital modulation such as amplitude shift keying, frequency shift keying, phase shift keying, or pulse code modulation and their variations. The principle of operations and various schematics of the modulators for different modulation schemes including Class S modulator for pulse-width modulation are described. Finally, the concept of time and frequency division multiplexing is introduced, as well as a brief description of different multiple access techniques.

A basic theory describing the operational principles of frequency conversion in receivers and transmitters is given in Chapter 7. The different types of mixers, from the simplest based on a single diode to a balanced and double-balanced type based on both diodes and transistors, are described and analyzed. The special case is a mixer based on a dual-gate transistor that provides better isolation between signal paths and simple implementation. The frequency multipliers that historically were a very important part of the vacuum-tube transmitters can extend the operating frequency range.

Chapter 8 presents the principles of oscillator design, including start-up and steady-state operation conditions, noise and stability of oscillations, basic oscillator configurations using lumped and transmission-line elements, and simplified equation-based oscillator analyses and optimum design techniques. An immittance design approach is introduced and applied to the series and parallel feedback oscillators, including circuit design and simulation aspects. Voltage-controlled oscillators and their varactor tuning range and linearity for different oscillator configurations are discussed. Finally, the basic circuits and operation principles of crystal and dielectric resonator oscillators are given.

Chapter 9 begins with description of the basic phase-locked loop concept. Then, the basic performance and structures of the analog, charge-pump, and digital phase-locked loops are analyzed. The basic loop components such as phase detector, loop filter, frequency divider, and voltage-controlled oscillator are discussed, as well as loop dynamic parameters. The possibility and particular realizations of the phase modulation using phase-locked loops are presented. Finally, general classes of frequency synthesizer techniques such as direct analog synthesis, indirect synthesis, and direct digital synthesis are discussed. The proper choice of the synthesizer type is based on the number of frequencies, frequency spacing, frequency switching time, noise, spurious level, particular technology, and cost.

Chapter 10 introduces the fundamentals of the power amplifier design, which is generally a complicated procedure when it is necessary to provide simultaneously accurate active device modeling, effective impedance matching depending on the technical requirements and operation conditions, stability in operation, and simplicity in practical implementation. The quality of the power amplifier design is evaluated by realized maximum power gain under stable operation condition with minimum amplifier stages, and the requirement of linearity or high efficiency can be considered where it is needed. For a stable operation, it is necessary to evaluate the operating frequency domains where the active device may be potentially unstable. To avoid the parasitic oscillations, the stabilization circuit technique for different frequency domains (from low frequencies up to high frequencies close to the device transition frequency) is discussed. The key parameter of the power amplifier is its linearity, which is very important for many wireless communication applications. The relationships between the output power, 1-dB gain compression point, third-order intercept point, and intermodulation distortions of the third and higher orders are given and illustrated for different active devices. The device bias conditions, which are generally different for linearity or efficiency improvement, depend on the power amplifier operation class and the type of the active device. The basic Classes A, AB, B, and C of the power amplifier operation are introduced, analyzed, and illustrated. The principles and design of the push-pull amplifiers using balanced transistors, as well as broadband and distributed power amplifiers, are discussed. Harmonic-control techniques for designing microwave power amplifiers are given with description of a systematic procedure of multiharmonic load-pull simulation using the harmonic balance method and active load-pull measurement system. Finally, the concept of thermal resistance is introduced and heatsink design issues are discussed.

Modern commercial and military communication systems require the high-efficiency long-term operating conditions. Chapter 11 describes in detail the possible circuit solutions to provide a high-efficiency power amplifier operation based on using Class D, Class F, Class E, or their newly developed subclasses depending on the technical requirements. In all cases, an efficiency improvement in practical implementation is achieved by providing the nonlinear operation conditions when an active device can simultaneously operate in pinch-off, active, and saturation regions, resulting in nonsinusoidal collector current and voltage waveforms, symmetrical for Class D and Class F and asymmetrical for Class E (DE, FE) operation modes. In Class F amplifiers analyzed in frequency domain, the fundamental-frequency and harmonic load impedances are optimized by short-circuit termination and open-circuit peaking to control the voltage and current waveforms at the device output to obtain maximum efficiency. In Class E amplifiers analyzed in time domain, an efficiency improvement is achieved by realizing the on/off active device switching operation (the pinch-off and saturation modes) with special current and voltage waveforms so that high voltage and high current do not concur at the same time.

In modern wireless communication systems, it is very important to realize both high-efficiency and linear operation of the power amplifiers. Chapter 12 describes a variety of techniques and approaches that can improve the power amplifier performance. To increase efficiency over power backoff range, the Doherty, outphasing, and envelope-tracking power amplifier architectures, as well as switched multipath power amplifier configurations, are discussed and analyzed. There are several linearization techniques that provide linearization of both entire transmitter system and individual power amplifier. Feedforward, cross cancellation, or reflect forward linearization techniques are available technologies for satellite and cellular base station applications achieving very high linearity levels. The practical realization of these techniques is quite complicated and very sensitive to both the feedback loop imbalance and the parameters of its individual components. Analog predistortion linearization technique is the simplest form of power amplifier linearization and can be used for handset application, although significant linearity improvement is difficult to realize. Different types of the feedback linearization approaches, together with digital linearization techniques, are very attractive to be used in handset or base station transmitters. Finally, the potential semidigital and digital amplification approaches are discussed with their architectural advantages and problems in practical implementation.

Chapter 13 discusses the circuit schematics and main properties of the semiconductor control circuits that are usually characterized by small size, low power consumption, high-speed performance, and operating life. Generally, they can be built based on the p-i-n diodes, silicon MOSFET, or GaAs MESFET transistors and can be divided into two basic parts: amplitude and phase control circuits. The control circuits are necessary to protect high power devices from excessive peak voltage or

dc current conditions. They are also used as switching elements for directing signal between different transmitting paths, as variable gain amplifiers to stabilize transmitter output power, as attenuators and phase shifters to change the amplitude and phase of the transmitting signal paths in array systems, or as limiters to protect power-sensitive components.

Finally, Chapter 14 describes the different types of radio transmitter architectures, history of radio communication, conventional types of radio transmission, and modern communication systems. Amplitude-modulated transmitters representing the oldest technique for radio communication are based on high- or low-level modulation methods, with particular case of an amplitude keying. Single-sideband transmitters as the next-generation transmitters could provide higher efficiency due to the transmission of a single sideband only. Frequency-modulated transmitters include different modulation techniques for transmitting audio and video information, both analog and digital. Wireless communication transmitters as a part of the cellular technologies provide a worldwide wireless radio access. Radar transmitters are required for many commercial and military applications such as phased-array radars, automotive radars, or electronic warfare systems. Satellite transmission systems contribute to worldwide transmission of any communication signals through satellite transmission is very attractive for their low-cost and low-power communication applications, occupying a very wide frequency range.

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Andrei Grebennikov

### INTRODUCTION

A vacuum-tube or solid-state radio transmitter is essentially a source of a radio-frequency (RF) signal to be transmitted through antenna in different radio systems such as wireless communication, television (TV) and broadcasting, navigation, radar, or satellite, the information format and electrical performance of which should satisfy the corresponding standard requirements. The transmission of radio signals is produced by modulation of different types, with different output power and transmission mode, and in different frequency ranges, from high frequencies to millimeter waves. Transmitters in which the power output is generated directly by the modulated source are considered as possessing high-level modulation systems. In contrast, arrangements in which the modulation systems.

Figure I.1 shows the simplified block diagram of a conventional radio transmitter intended to operate at radio and microwave frequencies, which consists of the following: the source of the information signal, which is usually amplified, filtered, or transformed to the intermediate frequency; the local oscillator and frequency multiplier, which establish the stabilized carrier frequency or some multiple of it; the RF modulator or mixer, which combines the signal and carrier frequency components to produce one of the varieties of the RF modulated waves; the power amplifier to deliver the RF modulated signal of required power level to the antenna; the antenna duplexer to separate and isolate transmitting and receiving paths. The power amplifier usually consists of cascaded gain stages, and each stage should have adequate linearity in the case of transmitting signal with variable amplitude corresponding to amplitude-modulated or multicarrier signals. In practice, there are many variations in transmitter architectures depending on the particular frequency bandwidth, output power, or modulation scheme.

Dr. Lee De Forest was an inventor who changed the world with electronics by inventing the vacuum tube, which he called the *audion*. In January 1907, De Forest filed a patent for an oscillation detector based on a three-electrode device representing a vacuum tube [1]. His pioneering innovation was the insertion of a third electrode (grid) in between the cathode (filament) and the anode (plate) of the previously invented diode. However, it was not until 1911 that De Forest built the first vacuum-tube amplifier based on three audions as amplifiers [2]. The original audion was capable of slightly amplifying received signals, but at this stage could not be used for more advanced applications such as radio transmitters. The inefficient design of the original audion meant that it was initially of little value to radio, and due to its high cost and short life it was rarely used. Eventually, vacuum-tube design was improved enough to make vacuum tubes more than novelties. Beginning in 1912, various researchers discovered that properly constructed (i.e., according to scientific and engineering principles) vacuum tubes could be employed in electrical circuits that made radio receivers and amplifiers thousands of times more powerful, and could also be used to make compact and efficient radio transmitters, which for the first time made radio broadcasting practical.

In 1914, the first vacuum-tube radio transmitters began to appear—a key technical development that would lead to the introduction of widespread broadcasting. Both amateurs and commercial firms started to experiment with the new vacuum-tube transmitters, employing them for a variety of purposes. Six years after suspending his efforts to make audio transmissions, when he had unsuccessfully

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FIGURE I.1 Conventional transmitter architecture.

tried to use arc-transmitters, De Forest again took up developing radio to transmit sounds, including broadcasting news and entertainment, this time with much more success. He demonstrated that with this form of transmitter it was possible to telephone one to three miles, and by means of the small 3.5-V amplifier tube used with this apparatus, direct current could be transformed to alternating current at frequencies from 60 cycles per second to 1,000,000 cycles per second [3]. It is interesting that De Forest recognized the irony that he had overlooked the potential of developing his audion as a radio transmitter at the beginning. Reviewing his earlier arc-transmitter efforts, he wrote in his autobiography that he had been "totally unaware of the fact that in the little audion tube, which I was then using only as a radio detector, lay dormant the principle of oscillation which, had I but realized it, would have caused me to unceremoniously dump into the ash can all of the fine arc mechanisms which I had ever constructed, a procedure which a few years later actually took place all over the world" [4]. Meanwhile, in June 1915, the American Telephone & Telegraph Company installed a powerful experimental vacuum-tube transmitter in Arlington, Virginia, which quickly achieved remarkable distances for its audio transmissions [5]. The Marconi companies joined those experimenting with



PHOTO I.1 Lee De Forest.

the new vacuum-tube transmitters, achieving an oversea working range of 50 km between ship aerials [6]. With the capable assistance of engineers including H. Round and C. Franklin, Guglielmo Marconi began experimenting with shortwave vacuum-tube transmitters by about 1916 [7].

However, Alexander Meissner was the first to amplify high-frequency radio signals by using a regenerative (positive) feedback in a vacuum triode. This principle of reactive coupling, which was given in its general form by Meissner in March 1913, later became the basis of the radio transmitter development [8]. The first high-frequency vacuum tube transmitters of small power up to 15 W were built by the Telefunken Company at the beginning of 1915. To provide high operating efficiency of the transmitter, the plate current of the special wave form, or else an auxiliary voltage of triple frequency, was impressed on the grid; thus greatly reducing the losses because, at the time when the highest voltages are applied to the tube, the passage of current through it is prevented. At the very beginning of 1920s, 1-kW transmitters had already been in use for radio telephony and telegraphy in several of the larger German cities. Much higher transmitting power was achieved by connecting in parallel eight or more tubes, each delivering 1.5 kW. In Russia during 1920, the 5.5-kW radio transmitter, where the modulated oscillations were amplified by a tube and transferred to the grids of six tubes in parallel that fed the antenna of 120-meter height, covered long distances of more than 4500 km [9]. An attempt in the field of radio television had been tried out in 1920 in order to provide a radio transmission of photographs with two antennas: one of which sends the synchronizing signal while the other sends the actual picture.

Edwin H. Armstrong is widely regarded as one of the foremost contributors to the field of radio engineering, being responsible for the regenerative circuit (1912), the superheterodyne circuit (1918), and the complete frequency-modulation radio broadcasting system (1933). Armstrong studied the audion for several years, performed extensive measurements, and understood and explained its operation when he devised a circuit, in which part of the current at the plate was fed back to the grid to strengthen the incoming signal. This discovery led to the independent invention of regeneration (or feedback) principle and the vacuum-tube oscillator. He then disproved the currently accepted theory



PHOTO I.2 Alexander Meissner.

#### 4 INTRODUCTION



PHOTO I.3 Edwin Armstrong.

of the action of the triode (three-electrode vacuum tube), and published the correct explanation in 1914 [10].

At the same time, the theoretical development of quantum mechanics during the 1920s played an important role in driving solid-state electronics, with understanding of the differences between metals, insulators, and semiconductors [11]. These continuing theoretical efforts then quickly led to the discovery of new devices, when Julius Lilienfeld invented the concept of a field-effect transistor in 1926 [12]. He believed that applying a voltage to a poorly conducting material would change its conductivity and thereby achieve amplification, but no one was able to do anything practically with this device until much later time. In conjunction with this, it is worth mentioning that the oscillating crystal detector was described by W. Eccles in 1909 and then practically implemented as an oscillator and even a low-power transmitter (based on one-port negative resistance principle) by O. Losev in early 1920s [13,14]. All details needed to duplicate these circuits to make a tunnel-diode oscillator were reported in the September 1924 issue of *Radio News* and in the 1st and 8th October 1924 issues of *Wireless World*, with predictions that crystals would someday replace valves in electronics.

Shortly after the end of the war in 1945, Bell Labs formed a Solid State Physics Group led by William Shockley, with an assignment to seek a solid-state alternative to fragile glass vacuumtube amplifiers. This group made a very important decision right at the beginning: that the simplest semiconductors were silicon and germanium and that their efforts would be directed at those two elements. The first attempts were based on Shockley's ideas about using an external electrical field on a semiconductor to affect its conductivity, but these experiments failed every time in all sorts of configurations and materials. The group was at a standstill until John Bardeen suggested a theory that invoked surface states that prevented the field from penetrating the semiconductor. In November 1947, John Bardeen and Walter Brattain, working without Shockley, succeeded in creating a point-contact transistor that achieved amplification when electrical field was applied to a crystal of germanium [15]. At the same time, Shockley secretly continued and successfully finished his own work to build a different sort of transistor based on n-p junctions that depended on the introduction of the minority carriers instead of point contacts, which he expected would be more



PHOTO I.4 William Shockley.

likely to be commercially viable [16]. In his seminal work *Electrons and Holes in Semiconductors with Applications to Transistor Electronics* (1955), Shockley worked out the critical ideas of drift and diffusion and the differential equations that govern the flow of electrons in solid-state crystals, where the Shockley ideal diode equation was also described. The term "transistor" was coined by John Pierce, who later recalled: "... at that time, it was supposed to be the dual of the vacuum tube. The vacuum tube had *transconductance*, so the transistor would have *transresistance*. And the name should fit in with the names of other devices, such as *varistor* and *thermistor*. And ... I suggested the name *transistor*."

The first to perceive the possibility of integrated circuits based upon semiconductor technology was Geoffrey Dummer, who said addressing the Electronic Components Conference in 1952: "With the advent of the transistor and the work in semiconductors generally, it seems now possible to envisage electronic equipment in a solid block with no connecting wires. The block may consist of layers of insulating, conducting, rectifying, and amplifying materials, the electrical functions being connected directly by cutting out areas of the various layers" [17]. In 1958, Jack Kilby of Texas Instruments developed the first integrated circuit consisting of a few mesa transistors, diffused capacitors, and bulk resistors on a piece of germanium using gold wires for interconnections [18]. The integrated circuit developed by Robert Noyce of Fairchild could resolve problems with wires by adding a final metal layer and then taking away some of it so that the wires required for the components to be connected were shaped so as to make the integrated circuit more suitable for mass production [19]. A year later, a planar process was developed by Jean Hoerni that utilized heat diffusion process, and oxide passivation of the surface protected the junctions and provided a reproducibility that assured more consistency than any previous manufacturing process. The first microwave gallium-arsenide (GaAs) Schottky-gate field-effect transistor (metal semiconductor field-effect transistor or MESFET), which had a maximum frequency  $f_{\text{max}} = 3$  GHz, was reported in 1967 [20]. But it was not until 1976 that the first fully monolithic single-stage GaAs MESFET X-band broadband amplifier was developed based on lumped matching elements [21]. Eight years later, on a GaAs chip of approximately the same area, an entire X-band transmit-receive (T/R) module was fabricated, consisting of two switches, a four-bit

Band	Frequency	Wavelength
HF (high frequency)	3-30 MHz	100–10 m
VHF (very high frequency)	30-300 MHz	10–1.0 m
UHF (ultra high frequency)	300-1000 MHz	1.0 m to 30 cm
L	1–2 GHz	30–15 cm
S	2–4 GHz	15 cm to 7.5 cm
С	4–8 GHz	7.50–3.75 cm
Х	8-12 GHz	3.75–2.50 cm
Ku	12–18 GHz	2.50-1.67 cm
K	18–27 GHz	1.67-1.11 cm
Ka	27–40 GHz	1.11 cm to 7.5 mm
V	40–75 GHz	7.5–4.0 mm
W	75–110 GHz	4.0-2.7 mm
Millimeter wave	110-300 GHz	2.7-1.0 mm

TABLE I.1 IEEE Standard Letter Designations for Frequency Bands.

phase shifter, a three-stage low-noise amplifier, and a four-stage power amplifier [22]. Generally, a monolithic microwave integrated circuit (MMIC) was defined as an active or passive microwave circuit formed in situ on a semiconductor substrate by a combination of deposition techniques including diffusion, evaporation, epitaxy, and other means [23].

Table I.1 shows the IEEE standard letter designations for frequency bands [24]. In military radar band designations, millimeter-wave bandwidth occupies the frequency range from 40 to 300 GHz. The letter designations (L, S, C, X, Ku, K, Ka) were meant to be used for radar, but have become commonly used for other microwave frequency applications. The K-band is the middle band (18–27 GHz) that originated from the German word "Kurz", which means short, while Ku-band is lower in frequency (Kurz-under), and Ka-band is higher in frequency (Kurz-above). The 1984 revision defined the application of letters V and W to a portion of the millimeter-wave region each while retaining the previous letter designators for frequencies.

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# **1** Passive Elements and Circuit Theory

The two-port equivalent circuits are widely used in radio frequency (RF) and microwave circuit design to describe the electrical behavior of both active devices and passive networks [1–4]. The two-port network impedance Z-parameters, admittance Y-parameters, or hybrid H-parameters are very important to characterize the nonlinear properties of the active devices, bipolar or field-effect transistors. The transmission *ABCD*-parameters of a two-port network are very convenient for designing the distributed circuits like transmission lines or cascaded elements. The scattering S-parameters are useful to characterize linear circuits, and are required to simplify the measurement procedure. Transmission lines are widely used in matching circuits in power amplifiers, in resonant circuits in the oscillators, filters, directional couplers, power combiners, and dividers. The design formulas and curves are presented for several types of transmission lines including stripline, microstrip line, slotline, and coplanar waveguide. Monolithic implementation of lumped inductors and capacitors is usually required at microwave frequencies and for portable devices. Knowledge of noise phenomena, such as the noise figure, additive white noise, low-frequency fluctuations, or flicker noise in active or passive elements, is very important for the oscillator modeling in particular and entire transmitter design in general.

#### 1.1 IMMITTANCE TWO-PORT NETWORK PARAMETERS

The basic diagram of a two-port nonautonomous transmission system can be represented by the equivalent circuit shown in Figure 1.1, where  $V_S$  is the independent voltage source,  $Z_S$  is the source impedance, LN is the linear time-invariant two-port network without independent source, and  $Z_L$  is the load impedance. The two independent phasor currents  $I_1$  and  $I_2$  (flowing across input and output terminals) and phasor voltages  $V_1$  and  $V_2$  characterize such a two-port network. For autonomous oscillator systems, in order to provide an appropriate analysis in the frequency domain of the two-port network in the negative one-port representation, it is sufficient to set the source impedance to infinity. For a power amplifier or oscillator design, the elements of the matching or resonant circuits, which are assumed to be linear or appropriately linearized, can be found among the LN-network elements, or additional two-port linear networks can be used to describe their frequency domain behavior.

For a two-port network, the following equations can be considered to be imposed boundary conditions:

$$V_1 + Z_S I_1 = V_S (1.1)$$

$$V_2 + Z_L I_2 = V_L. (1.2)$$

Suppose that it is possible to obtain a unique solution for the linear time-invariant circuit shown in Figure 1.1. Then the two linearly independent equations, which describe the general two-port network

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FIGURE 1.1 Basic diagram of two-port nonautonomous transmission system.

in terms of circuit variables  $V_1$ ,  $V_2$ ,  $I_1$ , and  $I_2$ , can be expressed in a matrix form as

$$[M][V] + [N][I] = 0 (1.3)$$

or

$$\left. \begin{array}{c} m_{11}V_1 + m_{12}V_2 + n_{11}I_1 + n_{12}I_2 = 0\\ m_{21}V_1 + m_{22}V_2 + n_{21}I_1 + n_{22}I_2 = 0 \end{array} \right\}.$$
(1.4)

The complex 2 × 2 matrices [*M*] and [*N*] in Eq. (1.3) are independent of the source and load impedances  $Z_{\rm S}$  and  $Z_{\rm L}$  and voltages  $V_{\rm S}$  and  $V_{\rm L}$ , respectively, and they depend only on the circuit elements inside the *LN* network.

If matrix [M] in Eq. (1.3) is nonsingular when  $|M| \neq 0$ , then this matrix equation can be rewritten in terms of [I] as

$$[V] = -[M]^{-1}[N][I] = [Z][I]$$
(1.5)

where [Z] is the open-circuit impedance two-port network matrix. In a scalar form, matrix Eq. (1.5) is given by

$$V_1 = Z_{11}I_1 + Z_{12}I_2 \tag{1.6}$$

$$V_2 = Z_{21}I_1 + Z_{22}I_2 \tag{1.7}$$

where  $Z_{11}$  and  $Z_{22}$  are the open-circuit driving-point impedances, and  $Z_{12}$  and  $Z_{21}$  are the open-circuit transfer impedances of the two-port network. The voltage components  $V_1$  and  $V_2$  due to the input current  $I_1$  can be found by setting  $I_2 = 0$  in Eqs. (1.6) and (1.7), resulting in an open-output terminal. Similarly, the same voltage components  $V_1$  and  $V_2$  are determined by setting  $I_1 = 0$  when the input terminal becomes open-circuited. The resulting driving-point impedances can be written as

$$Z_{11} = \frac{V_1}{I_1} \bigg|_{I_2=0} \quad Z_{22} = \frac{V_2}{I_2} \bigg|_{I_1=0}$$
(1.8)

whereas the two transfer impedances are

$$Z_{21} = \frac{V_2}{I_1} \bigg|_{I_2=0} \qquad Z_{12} = \frac{V_1}{I_2} \bigg|_{I_1=0}.$$
(1.9)

Dual analysis can be used to derive the short-circuit admittance matrix when the current components  $I_1$  and  $I_2$  are considered as outputs caused by  $V_1$  and  $V_2$ . If matrix [N] in Eq. (1.3) is nonsingular

when  $|N| \neq 0$ , this matrix equation can be rewritten in terms of [V] as

$$[I] = -[N]^{-1}[M][V] = [Y][V]$$
(1.10)

where [Y] is the short-circuit admittance two-port network matrix. In a scalar form, matrix Eq. (1.10) is written as

$$I_1 = Y_{11}V_1 + Y_{12}V_2 \tag{1.11}$$

$$I_2 = Y_{21}V_1 + Y_{22}V_2 \tag{1.12}$$

where  $Y_{11}$  and  $Y_{22}$  are the short-circuit driving-point admittances, and  $Y_{12}$  and  $Y_{21}$  are the short-circuit transfer admittances of the two-port network. In this case, the current components  $I_1$  and  $I_2$  due to the input voltage source  $V_1$  are determined by setting  $V_2 = 0$  in Eqs. (1.11) and (1.12), thus creating a short output terminal. Similarly, the same current components  $I_1$  and  $I_2$  are determined by setting  $V_1 = 0$  when input terminal becomes short-circuited. As a result, the two driving-point admittances are

$$Y_{11} = \frac{I_1}{V_1} \bigg|_{V_2 = 0} \quad Y_{22} = \frac{I_2}{V_2} \bigg|_{V_1 = 0}$$
(1.13)

whereas the two transfer admittances are

$$Y_{21} = \frac{I_2}{V_1} \bigg|_{V_2 = 0} \quad Y_{12} = \frac{I_1}{V_2} \bigg|_{V_1 = 0}.$$
 (1.14)

In some cases, an equivalent two-port network representation can be redefined in order to express the voltage source  $V_1$  and output current  $I_2$  in terms of the input current  $I_1$  and output voltage  $V_2$ . If the submatrix

$$\begin{bmatrix} m_{11} & n_{12} \\ m_{21} & n_{22} \end{bmatrix}$$

given in Eq. (1.4) is nonsingular, then

$$\begin{bmatrix} V_1 \\ I_2 \end{bmatrix} = -\begin{bmatrix} m_{11} & n_{12} \\ m_{21} & n_{22} \end{bmatrix}^{-1} \begin{bmatrix} n_{11} & m_{12} \\ n_{21} & m_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ V_2 \end{bmatrix} = [H] \begin{bmatrix} I_1 \\ V_2 \end{bmatrix}$$
(1.15)

where [H] is the hybrid two-port network matrix. In a scalar form, it is best to represent matrix Eq. (1.15) as

$$V_1 = h_{11}I_1 + h_{12}V_2 \tag{1.16}$$

$$I_2 = h_{21}I_1 + h_{22}V_2 \tag{1.17}$$

where  $h_{11}$ ,  $h_{12}$ ,  $h_{21}$ , and  $h_{22}$  are the hybrid *H*-parameters. The voltage source  $V_1$  and current component  $I_2$  are determined by setting  $V_2 = 0$  for the short output terminal in Eqs. (1.16) and (1.17) as

$$h_{11} = \frac{V_1}{I_1} \bigg|_{V_2 = 0} \quad h_{21} = \left. \frac{I_2}{I_1} \right|_{V_2 = 0} \tag{1.18}$$

where  $h_{11}$  is the driving-point input impedance and  $h_{21}$  is the forward current transfer function. Similarly, the input voltage source  $V_1$  and output current  $I_2$  are determined by setting  $I_1 = 0$  when

#### 12 PASSIVE ELEMENTS AND CIRCUIT THEORY

input terminal becomes open-circuited as

$$h_{12} = \frac{V_1}{V_2} \Big|_{I_1=0} \quad h_{22} = \frac{I_2}{V_2} \Big|_{I_1=0}$$
(1.19)

where  $h_{12}$  is the reverse voltage transfer function and  $h_{22}$  is the driving-point output admittance.

The transmission parameters, often used for passive device analysis, are determined for the independent input voltage source  $V_1$  and input current  $I_1$  in terms of the output voltage  $V_2$  and output current  $I_2$ . In this case, if the submatrix

$$\begin{bmatrix} m_{11} & n_{11} \\ m_{21} & n_{21} \end{bmatrix}$$

given in Eq. (1.4) is nonsingular, we obtain

$$\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = -\begin{bmatrix} m_{11} & n_{11} \\ m_{21} & n_{21} \end{bmatrix}^{-1} \begin{bmatrix} m_{12} & n_{12} \\ m_{22} & n_{22} \end{bmatrix} \begin{bmatrix} V_2 \\ -I_2 \end{bmatrix} = \begin{bmatrix} ABCD \end{bmatrix} \begin{bmatrix} V_2 \\ -I_2 \end{bmatrix}$$
(1.20)

where [ABCD] is the forward transmission two-port network matrix. In a scalar form, we can write

$$V_1 = AV_2 - BI_2 \tag{1.21}$$

$$I_1 = CV_2 - DI_2 \tag{1.22}$$

where A, B, C, and D are the transmission parameters. The voltage source  $V_1$  and current component  $I_1$  are determined by setting  $I_2 = 0$  for the open output terminal in Eqs. (1.21) and (1.22) as

$$A = \frac{V_1}{V_2}\Big|_{I_2=0} \quad C = \frac{I_1}{V_2}\Big|_{I_2=0}$$
(1.23)

where A is the reverse voltage transfer function and C is the reverse transfer admittance. Similarly, the input independent variables  $V_1$  and  $I_1$  are determined by setting  $V_2 = 0$  when the output terminal is short-circuited as

$$B = \frac{V_1}{I_2}\Big|_{V_2=0} \qquad D = \frac{I_1}{I_2}\Big|_{V_2=0}$$
(1.24)

where *B* is the reverse transfer impedance and *D* is the reverse current transfer function. The reason a minus sign is associated with  $I_2$  in Eqs. (1.20) to (1.22) is that historically, for transmission networks, the input signal is considered as flowing to the input port whereas the output current flowing to the load. The direction of the current  $-I_2$  entering the load is shown in Figure 1.2.

The parameters describing the same two-port network through different two-port matrices (impedance, admittance, hybrid, or transmission) can be cross-converted, and the elements of each



FIGURE 1.2 Basic diagram of loaded two-port transmission system.