Wire Ropes
This book on wire ropes is dedicated mainly to all users of wire ropes – the construction engineers, operators and supervisors of machines and installations running on wire ropes – and it is divided into three main sections. The first section deals with the different types of wire rope and their component parts, the second looks into the effects of wire ropes under tensile forces (stationary ropes), while the third takes a look at the wire ropes under bending and tensile force (running ropes).

In addition to deriving the various tensile, bending and twisting stresses, the compression and the extensions, the book includes the findings and descriptions of a great number of detailed experiments, in particular those concerning rope endurance under fluctuating tension and bending and rope discard criteria. As far as possible, the test findings have been evaluated statistically so that not only the mean value but also the scattering is apparent.

It has been the main concern of this book to present the methods used to calculate the most important rope quantities (rope geometry, wire stresses in the rope under tension, bending and twist, rope elasticity module, rope torque, rope efficiency, the bearable number of load cycles or bending cycles and the discard number of wire breaks, etc.) as well as to explain how they are applied by means of a large number of calculations as examples.

Essentially, this book is a translation of the first three chapters of the book Drahtseile, which was also published by Springer-Verlag in the year 2000. The translation has been supplemented in many places by more recent findings and examples of calculations. My translation has been revised and polished by Mrs. Merryl Zepf, who has a good understanding of the project. I am extremely grateful for all her efforts.

It would not have been possible to create this book without the support and encouragement of the head of Stuttgart University’s Institut für Fördertechnik und Logistik (Institute for Mechanical Conveying and Handling and Logistics), Professor Dr.-Ing. K.-H. Wehking. He welcomed the opportunity to present in English the diverse findings originating from almost 80 years of rope research at the institute combined with more general knowledge about
wire ropes. I am extremely grateful to Professor Wehking for his advice and support and for being able to use the infrastructure of the institute.

There have also been many enlightening discussions held with Prof. em. Dr. techn. Prof. E.h. Franz Beisteiner, the former head of the institute. I would like to thank him very much indeed for his constant willingness to have a discussion and for his sound advice that helped to clarify many a point in question. Also, I would also like to thank all members of staff at the institute for their readiness to discuss details and especially for their willingness to help in solving promptly any computer problems that arose. Thanks also go to Dr. Christoph Baumann at Springer Verlag for his pleasant cooperation.

Putting together this compilation of what we know about wire ropes today – even though there are probably some gaps – was certainly made easier by the OIPEEC (Organisation pour L’Étude de L’Endurance des Cables). During the past few decades, the OIPEEC has developed into the most important forum for discussing questions in connection with wire ropes. I am very grateful to my colleagues at the OIPEEC for their very stimulating discussions. The same is true for the members of the DRAHTSEIL-VEREINIGUNG e.V. (Wire Rope Association, Germany). Furthermore, I would also like to thank those wire rope manufacturers who have been interested in and supportive of wire rope research from the very beginning and have been responsible for a great deal of technical information and practical assistance.

Even though extreme care is always taken, it is hardly possible to print a book that has absolutely no errors. This is true for this book as well. Because of this, I would like to point out that a list has been created where any printing errors or inaccuracies can be entered. The latest version of this list of corrections can be found in the internet under:

http://www.uni-stuttgart.de/ift/forschung/update.html

For particularly complicated calculations there are Excel programs that can be downloaded free of charge under the address:

http://www.uni-stuttgart.de/ift/forschung/berechnung.html

To make the list of corrections as comprehensive as possible, I would like to ask all readers for their assistance to report any mistakes found to the following address:

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1

Wire Ropes, Elements and Definitions

1.1 Steel Wire

The very high strength of the rope wires enables wire ropes to support large tensile forces and to run over sheaves with relative small diameters. Very high-strength steel wires had already been existence for more than a hundred years when patenting – a special heating process – was introduced and the drawing process perfected. Since then further improvements have only occurred in relatively small steps.

There are a number of books about the history of wire ropes and wire rope production beginning with its invention by Oberbergrat Wilhelm August Julius Albert in 1834 and one of these is by Benoit (1935). Newer interesting contributions on the history of wire ropes have been written by Verreet (1988) and Sayenga (1997, 2003).

A voluminous literature exists dealing with the manufacture, material and properties of rope wires. In the following, only the important facts will be presented, especially those that are important for using the wires in wire ropes.

1.1.1 Non-Alloy Steel

Steel wires for wire ropes are normally made of high-strength non-alloy carbon steel. The steel rods from which the wires are drawn or cold-rolled are listed in Table 1.1 as an excerpt of a great number of different steels from the European Standard EN 10016-2. The rods for rope wires have a high carbon content of 0.4–0.95%.

The number in the name of the steel gives the mean content of carbon in weight percent multiplied with the factor 100. For example, the steel name C 82 D means that the steel has a mean carbon content of 0.82%. Steels with high carbon content close to 0.86% with eutectoid fine perlite – a mix of cementite (Fe₃C) and ferrite – are preferred for rope wires.
Table 1.1. Non-alloy steel rod for drawing (excerpt of EN 10 016-2)

<table>
<thead>
<tr>
<th>Steel name</th>
<th>Steel number</th>
<th>Heat analysis carbon content (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>C 42 D</td>
<td>1.0541</td>
<td>0.40–0.45</td>
</tr>
<tr>
<td>C 48 D</td>
<td>1.0517</td>
<td>0.45–0.50</td>
</tr>
<tr>
<td>C 50 D</td>
<td>1.0586</td>
<td>0.48–0.53</td>
</tr>
<tr>
<td>C 82 D</td>
<td>1.0626</td>
<td>0.80–0.85</td>
</tr>
<tr>
<td>C 86 D</td>
<td>1.0616</td>
<td>0.83–0.88</td>
</tr>
<tr>
<td>C 88 D</td>
<td>1.0628</td>
<td>0.85–0.90</td>
</tr>
<tr>
<td>C 92 D</td>
<td>1.0618</td>
<td>0.90–0.95</td>
</tr>
</tbody>
</table>

Carbon steels only contain small quantities of other elements. EN 10016-2 gives the following limits for the chemical ingredients of carbon steel rods used for rope wires: Si 0.1–0.3%, Mn 0.5–0.8%, P and S <0.035%, Cr <0.15%, Ni <0.20%, Mo <0.05%, Cu <0.25% and Al <0.01%. The strength increases with an increasing carbon content and the breaking extension decreases if all other influences are constant. Higher contents of sulphur S, phosphorus P, chrome Cr and copper Cu reduce the steel’s ductility, Schneider (1973).

Usually, wires for wire ropes have a round cross-section. In special cases, however, wires with other cross-sections – called profile wires – are used. The different cross-sections are to be seen in Fig. 1.1. The profile wires in the upper row are inserted in locked coil ropes. The wires below are used for triangular and oval strands.

In wires with a high carbon content which had been aged artificially, Unterberg (1967) and Apel and Nümminghoff (1983) found a distinct decrease in the breaking extension and the number of turns from the torsion test. The

![Wire Cross-Sections](image)

**Fig. 1.1.** Wire cross-sections for wire ropes
1.1 Steel Wire

The number of test bendings is slightly reduced and the strength slightly increased. The finite life fatigue strength is partly increased or decreased.

Bending tests were repeated with three wire ropes after they had been in storage for 22 years. The original tests were well documented and the new tests were done in the same way with the usual lubrication. There was virtually no difference in the rope bending endurance documented for the original tests and the new tests. For two of these wire ropes, the mean strength of the wires was reduced during the long period of storage by a maximum of 3%. For one rope, the mean strength of the wires increased by 2.7%.

1.1.2 Wire Manufacturing

After the rod has been patented in a continuous system, the wire diameter is reduced in stages by cold drawing or cold rolling, rolling especially for profile wires. Patenting is a heating process. First the wire is heated in an austenising furnace at about 900°C. Then the temperature is abruptly reduced to about 500°C when the wire is put through a lead bath. After remaining there for a while, the wire then leaves the bath and enters the normal temperature of the surroundings. Figure 1.2 shows the course of the temperature during the patenting process. In recent times, the patenting process has partly been replaced by cooling in several stages while drawing or rolling the rod, Marcol (1986).

By patenting, the steel rod gets a sorbite structure (fine stripes of cementite and ferrite) which is very suitable for drawing. In the following drawing process, the wire cross-section is reduced in stages, for example in seven stages from 6 to 2 mm in diameter. After the wires have been patented, they can be drawn again. The quality of the wire surface can be improved by draw-peeling the wire rod, Kieselstein (2005).

![Fig. 1.2. The course of the temperature in the patenting process](image)
The principle of the wire drawing was described at an early date by Siebel (1959). The strength increases with the growing decrease of the cross-section by drawing and at the same time the breaking extension also decreases. The higher the carbon content of the wires, the stronger they are. For wires with small diameters below 0.8 mm, the strength can reach about 4,000 N/mm$^2$, for thicker wires about 2,500 N/mm$^2$, and in all cases the remaining ductility is low. The standardised nominal strengths of rope wires are

- $R_0 = 1,370$ N/mm$^2$ (in special cases)
- $R_0 = 1,570$ N/mm$^2$
- $R_0 = 1,770$ N/mm$^2$
- $R_0 = 1,960$ N/mm$^2$
- $R_0 = 2,160$ N/mm$^2$ (with a smaller wire diameter)
- $R_0 = 2,450$ N/mm$^2$ (with a smaller wire diameter).

The nominal strength is the minimum strength. The deviation allowed above the nominal strength is about 300 N/mm$^2$. However, the real deviation is usually much smaller.

1.1.3 Metallic Coating

Rope wires needing to be protected against corrosion are normally zinc coated. Zinc coating provides reliable protection against corrosion. Even if the zinc layer is partly damaged, the steel remains protected as the electro-chemical process results in the zinc corroding first. With zinc, the wires can be coated by hot zincing or a galvanizing process. With hot zincing, the outer layer consists of pure zinc. Between this layer and the steel wire there is a boundary layer of steel and zinc compounds. With zinc galvanized wires, the whole layer of the coating, which can be relatively thick, consists of pure zinc and has a smooth surface.

In most cases the wires are covered by hot zincing. The layer of FeZn-compounds should be avoided or at least kept thin as they are relatively brittle which can lead to cracks when the wire is bent. To keep the FeZn layer thin, the wires should only be left in the zinc bath (with a temperature 440–460°C) for a short time.

During the hot zincing, the strength of the wires is somewhat reduced Wyss (1956). Because of this, and also because of the rough surface resulting from the zincing, the wires are often drawn again. This process increases the strength of the wire again and the zinc surface is smoothed. Before drawing, the zinc layer should be thicker than required as part of the zinc layer will be lost during the drawing process.

Blanpain (1964) found that during the re-drawing the brittle Fe–Zn layer may tear especially if the Fe–Zn layer is relatively thick. The resulting gaps will be entered from inside by a steel arch and are not visible from outside as they are closed with zinc. The fatigue strength of these wires is reduced due to the sharp edges of the gaps.
As an alternative to zinc, the wires can be coated with galfan, an eutectoid zinc–aluminium alloy Zn95Al5 (95% zinc, 5% aluminium). Nünninghoff and Sczepanski (1987) and Nünninghoff (2003) found that this Zn–Al alloy offers better protection against corrosion than pure zinc. The Zn95Al5 coating also has the further advantage that the brittle Fe–Zn-layer is avoided. However, the Zn95Al5-layer is not as resistant to wear as the pure zinc layer which means that Zn95Al5-coated wires are not as suitable for running ropes.

In Table 1.2, the surface-related mass of zinc coating is listed as an excerpt of Table 1.1 of EN 10244-2 in different classes. For a very thick coating, a multiple of class A can be used, as for example A×3. A surface-related zinc mass of 100 g/m$^2$ means that the thickness of the zinc layer is about 0.015 mm. For the Zn95Al5 coating, EN 10244-2 provides nearly the same surface-related mass for the classes A, B and AB. Unlike EN 10244-2, in Table 1.2 and in the following the symbol $\delta$ is used for the diameter of the wire.

### 1.1.4 Corrosion Resistant Wires

In exceptional cases corrosion resistant wires (stainless steel) have been used as rope wires. Some corrosion resistant steels for wires are listed in Table 1.3 from prEN 10088-3: 2001. The steel names of these high alloy steels begin with the capital letter X. The following number gives the carbon content in % multiplied with the factor 100. Then the symbols and the contents in % of the alloy elements are given. For example, for the steel X5CrNiMo17-12-2 the contents are 0.05% carbon, 17% chromium, 12% nickel and 2% molybdenum.

#### Table 1.2. Surface-related mass of zinc coating (excerpt of EN 10 244-2)

<table>
<thead>
<tr>
<th>Wire diameter (mm)</th>
<th>A (g/m$^2$)</th>
<th>AB (g/m$^2$)</th>
<th>B (g/m$^2$)</th>
<th>C (g/m$^2$)</th>
<th>D (g/m$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.20 ≤ $\delta$ &lt; 0.25</td>
<td>30</td>
<td>20</td>
<td>20</td>
<td>20</td>
<td>15</td>
</tr>
<tr>
<td>0.50 ≤ $\delta$ &lt; 0.60</td>
<td>100</td>
<td>70</td>
<td>50</td>
<td>35</td>
<td>20</td>
</tr>
<tr>
<td>1.00 ≤ $\delta$ &lt; 1.20</td>
<td>165</td>
<td>115</td>
<td>80</td>
<td>60</td>
<td>25</td>
</tr>
<tr>
<td>1.85 ≤ $\delta$ &lt; 2.15</td>
<td>215</td>
<td>155</td>
<td>115</td>
<td>80</td>
<td>40</td>
</tr>
<tr>
<td>2.8 ≤ $\delta$ &lt; 3.2</td>
<td>255</td>
<td>195</td>
<td>135</td>
<td>100</td>
<td>50</td>
</tr>
<tr>
<td>4.4 ≤ $\delta$ &lt; 5.2</td>
<td>280</td>
<td>220</td>
<td>150</td>
<td>110</td>
<td>70</td>
</tr>
<tr>
<td>5.2 ≤ $\delta$ &lt; 8.2</td>
<td>290</td>
<td>–</td>
<td>–</td>
<td>110</td>
<td>80</td>
</tr>
</tbody>
</table>

#### Table 1.3. Strength of drawn wires out of corrosion resistant steel (excerpt of prEN 10 088-3:2001, Table 1.8)

<table>
<thead>
<tr>
<th>Steel name</th>
<th>Steel number</th>
<th>Strength range (N/mm$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>X10CrNi18-8</td>
<td>1.4310</td>
<td>600–800</td>
</tr>
<tr>
<td>X5CrNiMo17-12-2</td>
<td>1.4401</td>
<td>900–1100</td>
</tr>
<tr>
<td>X3CrNiMo17-13-3</td>
<td>1.4436</td>
<td>1,000–1,250</td>
</tr>
<tr>
<td>X1CrNiMoCuN20-18-7</td>
<td>1.4547</td>
<td>1,400–1,700</td>
</tr>
<tr>
<td>X1CrNi25-21</td>
<td>1.4335</td>
<td>1,600–1,900</td>
</tr>
</tbody>
</table>
Corrosion resistant wires for ropes have an austenite structure. Because of this structure they cannot be magnetized which means that the highly effective magnetic method of testing cannot be used to inspect the ropes. It should also be taken into consideration that these steels are not corrosion resistant in all environments.

Like non-alloy carbon steel wires, corrosion resistant steel wires are produced by drawing. The strength range stated in Table 1.3 is valid for drawn wires with a diameter $\geq 0.05$ mm. From the different corrosion resistant steels available usually those of medium strength are used. Corrosion resistant wire ropes running over sheaves are not usually as durable as those made of non-alloy carbon steel.

### 1.1.5 Wire Tensile Test

The tensile test is standardised according to EN 10002-1. The main results of the tensile test provide the measured tensile strength $R_m$ and the total extension $\varepsilon_t$. It is not possible to detect precisely the limit where the yielding of the wire begins. However, the yield strength is defined for a small residual extension. Here, the most frequently used extension is $\varepsilon = 0.2\%$ and the stress at this point is the yield strength $R_{po.2}$. The elasticity module can be evaluated with a special tensile test.

If only the tensile strength $R_m$ has to be evaluated, it can be done without straightening the wire. However, if the different extensions and the yield strength have to be evaluated too, the wire has to be straightened prior to testing. The measurement starts at a stress of about $10\%$ of the tensile strength $R_m$. Under this stress, the height of the wire bow at a distance measured of 100 mm should be smaller than 0.5 mm.

A typical stress–extension diagram of a straightened wire is shown in Fig. 1.3. It is possible to take the tensile strength $R_m$, the total extension $\varepsilon_t$ and the residual extension $\varepsilon_r$ directly from this figure. To determine the elasticity module $E$ and the yield strength $R_{po.2}$, the following method has to be used. After a certain yielding, the wire has to be unloaded and loaded again. As a result, a hysteresis loop occurs as seen in Fig. 1.4. A middle line of this hysteresis defines the elasticity module $E = \Delta \sigma / \Delta \varepsilon$. To evaluate the yield strength $R_{po.2}$, a parallel to the middle line of the hysteresis has to be drawn through the residual extension $\varepsilon_r = 0.2\%$ on the abscissa. Then the yield strength $R_{po.2}$ is found as an ordinate where the parallel meets the stress extension line.

To determine stresses, strengths and elasticity modules, the cross-section $A$ of the unloaded wire has to be measured very precisely. (Unlike EN 10002-1, the symbol A is used here for the cross-section.) The error in measurement of the cross-section should be $1\%$ at the most. For round wires the cross-section
1.1 Steel Wire

Fig. 1.3. Stress extension diagram of a straightened wire, $\delta = 1.06$ mm

Fig. 1.4. Evaluation of the yield strength $R_{p0.2}$ according to EN 10002-1
has to be calculated from two wire diameters $\delta$ measured perpendicular to each other.

To fulfill this accuracy requirement for the cross-section, the wire diameter $\delta$ should be measured with a maximum deviation of 0.5%. With commonly used measuring instruments this accuracy requirement can only be achieved for thicker wires. For thin wires and profile wires, the cross-section can be evaluated by weighing. With the wire weight $m$ in g, the wire length $l$ in mm and the density $\rho$, the cross-section is then

$$A = \frac{m}{l \cdot \rho}.$$  \hfill (1.1)

The density for steel is normally $\rho = 0.00785 \text{ g/mm}^3$. However, because of the great carbon content of wires used for wire ropes it is to use $\rho = 0.00780 \text{ g/mm}^3$.

The total extension of steel wires for ropes amounts to about $\varepsilon_t = 1.5-4\%$ and the yield strength $R_{p0.2}$ is about 75-95% of the measured tensile strength $R_m$. For wires taken out of ropes and straightened, the total extension is about $\varepsilon_t = 1.4-2.9\%$ and the yield strength $R_{p0.2}$ is about 85-99% of the tensile strength $R_m$, Schneider (1973).

Because of early yielding in parts of the cross-section of the non-straightened wires and even if the wires are straightened in the normal way, the elasticity module can only evaluated precisely enough if the wire has yielded before over the whole cross-section. However, that does not mean that the two parts of a broken wire resulting from a tensile test can be used for the evaluation of the elasticity module. These wire parts cannot be used because they may have new inherent stresses due to buckling from the wire breaking impact, Unterberg (1967).

For straightened wires from wire ropes, Wolf (1987) evaluated a mean elasticity module $E = 199,000 \text{ N/mm}^2$. For new wires, Häberle (1995) found the mean elasticity module $E = 195,000 \text{ N/mm}^2$. Together with other measurements – after loading the wires close to the breaking point – a mean elasticity module has been evaluated for the stress field of practical usage. This mean elasticity module of rope wires made of carbon steel in the following is $E = 196,000 \text{ N/mm}^2$.

The elasticity module decreases a little with larger upper stresses. For drawn corrosion resistant wires with the steel number 1.4310 and 1.4401, Schmidt and Dietrich (1982) evaluated the elasticity module $E = 160,000 \text{ N/mm}^2$, respectively, $E = 150,000 \text{ N/mm}^2$.

1.1.6 Wire Endurance and Fatigue Strength

Test Methods, Definitions

The wires in wire ropes are stressed by fluctuating tension, bending, pressure and torsion. For a long time wires have been tested in different testing
machines under one or a combination of these fluctuating stresses. The tests with combined stresses, especially bending and pressure, have been done with the aim to imitate the stresses in a wire rope. Such tests have been done by Pfister (1964); Lutz (1972), Pantucek (1977) and Haid (1983). However the test results do not come up to expectations, or only imperfectly. The wire endurance for example has even been increased when the wires – loaded by fluctuating bending – are loaded in addition by fluctuating pressure. This effect can probably be attributed to a strain hardening of the wire surface. An overview of the test methods with single or combined stresses has been described by Wolf (1987).

Nowadays, wire fatigue tests are normally tests with only one fluctuating stress – mostly a longitudinal stress. The test methods with fluctuating longitudinal stresses are:

- Tensile fatigue test (wire under fluctuating tensile force)
- Simple bending test (fluctuated bending of the wire over one sheave)
- Reverse bending test (fluctuating bending of the wire over two sheaves or sheave segments)
- Rotary bending test (wire bending by rotating the wire).

For these test methods, the principle wire arrangement in the test machines is shown in Fig. 1.5. The fluctuating longitudinal stress affects different zones of the wire cross-sections. The wire cross-sections with the zones of the highest fluctuating longitudinal stress are shown in Fig. 1.5 below the wire arrangements. The highest stressed zones are shaded. The highest fluctuating longitudinal stress is taken as the nominal fluctuating stress.

For fatigue strength (infinite life), instead of the stress the symbols $\sigma$ are written with indices as capital letters.

In Fig. 1.5, the stress amplitude $\sigma_a$ and the middle stress $\sigma_m$ are listed for general cases in fatigue tests. Below them the stresses are listed for the special cases alternate stress $\sigma_{alt}$ and repetitive stress $\sigma_{rep}$. Figure 1.6 shows the stress course over one load cycle with the stress amplitude $\sigma_a$ and the middle stress $\sigma_m$ for general cases. In a fatigue test, the endurance of the wire is counted by the number of load cycles $N$ it takes.

Figure 1.7 shows a Haigh-diagram with the abscissa for the constant middle stress $\sigma_m$ and the ordinate for the fluctuating strength $\sigma_A$ as amplitude around the middle stress $\sigma_m$. The special cases alternate and repetitive stresses are inserted. The alternate strength $\sigma_{Alt}$ is the amplitude for a middle stress $\sigma_m = 0$. The repetitive strength $\sigma_{Rep} = 2\sigma_A$ is the strength range for a middle stress $\sigma_m = \sigma_A$. That means for the repetitive strength $\sigma_{Rep}$ the lower stress is $\sigma_{lower} = 0$.

The two basic stresses are tensile stress

$$\sigma_t = S/A \quad (1.1a)$$
### 1 Wire Ropes, Elements and Definitions

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<th>simple bending</th>
<th>reverse bending</th>
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<th>zone of maximum fluctuating stress</th>
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<th>stress amplitude</th>
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<td>( \sigma_a = \sigma_{t,a} )</td>
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<td>( \sigma_{t,alt} ) with ( \sigma_{t,m} = 0 )</td>
<td>( \sigma_{t,rep} ) with ( \sigma_{t,m} = \sigma_{a,rep} )</td>
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<td>( \sigma_{a} = \sigma_{b}/2 )</td>
<td>( \sigma_{m} = \sigma_{t,m} + \sigma_{b}/2 )</td>
<td>( \sigma_{b,alt} ) with ( \sigma_{t,m} = 0 )</td>
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<td>( \sigma_{t,rep} ) with ( \sigma_{t,m} = \sigma_{b,rep}/2 )</td>
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**Fig. 1.5.** Wire arrangement for the fatigue tests, zone of maximum stress amplitude in the wire cross-section, stress amplitudes and middle stresses

**Fig. 1.6.** Stress course during a load cycle
and bending stress according Reuleaux (1861)

$$\sigma_b = \frac{\delta}{D} \cdot E.$$  \hspace{1cm} (1.1b)

In these equations $S$ is the tensile force, $A$ the wire cross-section and $\delta$ the wire diameter. $D$ is the curvature diameter of the wire centre on the sheave, which means $D = D_0 + \delta$, with the contact diameter $D_0$ between wire and sheave. $E$ is the elasticity module.

**Testing Machines**

*Tensile fatigue test.* Testing methods with fluctuating tensile forces for the testing of materials and components are very commonly used. For rope wires, such tests were started as early as those from Pomp and Hempel (1937). The wire terminations are the main problem in carrying out these tests. If a normal press clamp is used, the wire would mostly break in the clamp.

In order to find out the real endurance or the real tensile fatigue strength of the wire, the wire has to be fastened in such a way that the wire breaks in the free length. To do this, a lamella clamp is used where the tensile force is gradually transferred from lamella to lamella. In addition the wire ends – which are fastened in the clamps – are strain-hardened by a rolling process. During this process, the fatigue tensile strength of the wire ends is increased slightly over that of the wire in the free length. This hardening of the wire ends together with the lamella clamp provides a high probability that the wire breaks in the free length.

In the fluctuating tensile tests the stress is constant over the whole cross-section as shown in Fig. 1.5. The total stress is composed of a constant middle stress $\sigma_m$ and a stress amplitude $\sigma_a$,

$$\sigma = \sigma_m \pm \sigma_a.$$

Because of the risk of buckling, the stress amplitude $\sigma_a$ normally should be smaller than the middle stress $\sigma_m$. Tensile fatigue tests with a compressive section can only be done with very short wires.
Simple bending test, one sheave. In this method the wire moves over one sheave forwards and backwards, Woernle (1929), Donandt (1950) Müller (1961) etc. The wire is loaded by a constant tensile force $S$ and a fluctuating bending. For this test,

the middle stress is $\sigma_m = \sigma_{t,m} + \sigma_b/2$

and the stress amplitude is $\sigma_a = \sigma_b/2$.

The fluctuating bending stress $\sigma_b$ exists only in one small segment of the wire cross-section in the outside wire bow, as shown in Fig. 1.5. In the other small wire segment lying on the sheave, the bending stress is compressive. There is no wire breakage to be expected from this stress, especially if this stress is reduced – as is normal – by a tensile stress $\sigma_{t,m}$.

Reverse bending test, two sheaves. In this method the wire first moves over one sheave and then over a second sheave with reverse bending forwards and backwards, Schmidt (1964). In another method the wire is bent and reverse bent over sheave segments, Unterberg (1967). For both methods, the wire is loaded by a constant tensile force $S$ and a fluctuating bending. For the wire reverse bending test

the middle stress is $\sigma_m = \sigma_{t,m}$

and the stress amplitude is $\sigma_a = \sigma_b$.

The fluctuating bending stress $\sigma_b$ exists only in two small segments of the wire cross-section, as shown in Fig. 1.5.

The pressure between the wire and the single sheave or two sheaves is small and can be neglected. The advantage of this bending test method is that the tensile stress $\sigma_m$, and the bending stress can be chosen quite freely. There should be only a tensile force chosen that is large enough to ensure that the wire lies securely on the sheave in contact with the bow.

Rotary bending test. In a rotary bending machine, the wire is bent in a free bow around its own axis. By turning the wire, the stress in an outer fibre of the bent wire changes from compressive to tensile stress and back again. In one turn of the wire around the wire axis, each of the outside fibres of the wire is stressed by a complete cycle of longitudinal stress. The stress amplitude $\pm \sigma_a$ decreases linearly from the outside of the wire to the wire axis. Therefore – as shown in Fig. 1.5 – the maximum (nominal) stress exists only in a small ring zone. The advantage of rotary bending tests is that it can be done very quickly with a frequency of 50 and more turns/second.

Older bending machines which rotate the wire are the Haigh/Robertson machine, NN (1933), the Schenck machine, Erlinger (1942) and the Hunter testing machine, Votta (1948). These machines have the disadvantage that of the whole wire length only a small part is bent with the maximal (nominal) bending stress $\sigma_a$. The newer Stuttgart rotary bending machine, Fig. 1.8, avoids this disadvantage, Wolf (1987). In this machine the wire has almost the same bending stress for the whole bending length. The wire bow between the two parallel axes of the rotating wire terminations with the distance $C$ is nearly a circular arc. One of the two wire terminations is driven.
One slight disadvantage of both the Hunter testing machine and the Stuttgart testing machine is that the bending length is determined by the chosen bending stress. The great advantage of these two machines is, however, that the bending stress is determined by geometric dimensions only and these can be measured very simply.

For the Stuttgart rotary bending machine, the bending length (free wire length between the terminations) $l$ is only slightly larger than the circle bow length $C\pi/2$. Therefore the bending stress on the terminations is only slightly smaller than in the middle of the bending length. This means that wire breakage in or close to the terminations is almost certainly avoided and the bending stress is nearly constant over the whole of the bending length. Figure 1.9 shows the bending stress along the bending length in the Schenck machine and the Stuttgart machine.

The bending stress amplitude in the middle of the bending length $l$ (free wire length) is

$$\sigma_a = \sigma_b = \frac{k \cdot \delta \cdot E}{C} \quad \text{(1.1c)}$$
This bending stress, the maximum stress, is taken as the nominal bending stress of the wire in the Stuttgart rotary bending machine. The minimum bending stress on both of the wire terminations is

$$\sigma_{b,\text{min}} = \frac{k_0 \cdot \delta \cdot E}{C}.$$  \hspace{1cm} (1.1d)

For both equations: $k$ and $k_0$ are constants in Table 1.4, $\delta$ is the wire diameter, $E$ is the elasticity module and $C$ is the distance between the parallel axes of the wire terminations.

Furthermore, in Table 1.4, the ratio of the minimum and the nominal bending stress $\sigma_{b,\text{min}}/\sigma_b$ is listed. For his tests Wolf (1987) used the ratio $l/C = 1.6$ instead of $\pi/2$ with the minimum stress $\sigma_{b,\text{min}} = 0.883 \cdot \sigma_b$ or a 11.7% smaller stress at the wire terminations. Later on, it was shown in a great number of tests that in practically all cases where the ratio is $l/C = 1.58$ the wires break in the free wire length. Since 1990, therefore, all the tests with the Stuttgart rotary bending machine have been done with the ratio $l/C = 1.58$. Because of the very small stress reduction of only 4% at the wire terminations, the maximum bending stress amplitude can be considered as stress over the whole bending length.
The middle stress is practically $\sigma_m \approx 0$. As an example for the ratio $l/C = 1.58$ and the bending stress $\sigma_b = 600 \text{ N/mm}^2$, the compressive stress is only $\sigma_m = 965 \cdot (\delta/C)^2 = 0.0089 \text{ N/mm}^2$.

**Wöhler Diagram**

Wolf (1987) did a great number of fatigue tests with the simple Stuttgart rotary bending machine using wires taken from wire ropes. He straightened all the wires in the same way with a special device before conducting the fatigue tests. Fig. 1.10 shows the numbers of bending cycles $N$ resulting from a series of tests with wires of 1 mm diameter taken from Seale ropes for varying amplitude of the rotary bending stress (alternate bending stress on the whole circumference) $\sigma_{rot} \approx \sigma_{b,alt}$. For the logarithm normal distribution of the bending cycles $N$, the standard deviation increases in the usual way with decreasing bending stress amplitude $\sigma_{rot}$.

Wolf (1987) transferred this number of bending cycles to a Wöhler diagram as shown in Fig. 1.11. In the Wöhler diagram, he drew a line for the mean number of bending cycles and lines for 5 and 95% of the breaking probability. The mean rotary bending strength (infinite life fatigue strength) for wires in 12 Seale ropes is $\bar{\sigma}_{rot} = \pm 640 \text{ N/mm}^2$. In the Wöhler diagram shown in Fig. 1.12, the number of rotary bending cycles for 0.95 mm diameter wires

![Wöhler Diagram](image-url)
Fig. 1.11. Wöhler-diagram for wires, diameter $\delta = 1\ mm$, from Seale ropes, Wolf (1987)

Fig. 1.12. Wöhler-diagram for wires, diameter $\delta = 0.95\ mm$, from Warrington ropes, Wolf (1987)

taken from 20 Warrington ropes has been transferred in the same way. The mean rotary bending strength is $\sigma_{\text{Rot}} = \pm 640\ \text{N/mm}^2$. The deviation for the number of rotary bending cycles $N$ and for the rotary bending strength $\sigma_{\text{Rot}}$ is much smaller than in the Wöhler-diagram in Fig. 1.11.

For both wires, the transition from the finite to the infinite life strength lies at the number of bending cycles of about $N = 300,000$. This is situated in the range between $N = 150,000$ and $N = 500,000$ that Hempel (1957) and Unterberg (1967) previously found in rotary bending and fluctuating tensile tests.
Finite Wire Endurance

For straightened wires taken from wire ropes, Wolf (1987) evaluated a mean number of rotary bending cycles for wires with diameter $\delta = 0.8–1.0$ mm
\[
\lg \bar{N} = 21.708 - 5.813 \cdot \lg \sigma_{\text{rot}}. \quad (1.2a)
\]
Briem (2000) Ziegler, Vogel and Wehking (2005) have also done a great number of fatigue tests with a Stuttgart rotary bending machine. In both series of fatigue tests the wires were new (not taken from a rope). They were only straightened before the tests. The following endurance equations were found by regression calculation using the test results in the finite life region: Briem (2000)
\[
\lg \bar{N} = 13.74 - 3.243 \cdot \lg \sigma_{\text{rot}} - 0.30 \cdot \lg \delta - 0.74 \cdot \lg \frac{R_0}{1770} \quad (1.2b)
\]
for wire diameters $\delta = 0.8 – 2.2$ mm and
for nominal strength $R_0 = 1,770; 1,960; \text{and} 2,160 \text{N/mm}^2$.
Ziegler, Vogel, Wehking (2005) found
\[
\lg \bar{N} = 12.577 - 3.542 \cdot \lg \sigma_{\text{rot}} - 0.072 \cdot \lg \delta - 0.612 \cdot \lg R_m \quad (1.2c)
\]
for wire diameters $\delta = 0.8–1.8$ mm and
for nominal strength $R_0 = 1,370–2,160 \text{N/mm}^2$.
The influence of the diameter of the wire and its tensile strength is different in the two equations. Briem (2000) even found that the number of rotary bending cycles is reduced when the tensile strength is increased. Only the bending stress as a main influence may be considered as a common result because of the relatively small range of wire diameters and tensile strength tested. Thus, the mean number of rotary bending cycles for new wires with a diameter $\delta = 1$ mm and tensile strength $R_0 = 1,770 \text{N/mm}^2$ is
\[
\lg \bar{N} = 14.152 - 3.393 \cdot \lg \sigma_{\text{rot}}. \quad (1.2d)
\]
According to these equations with rotary bending stress $\sigma_{\text{rot}} = \pm 900 \text{N/mm}^2$ as an example, the mean number of bending cycles for new wires is $N = 13,000$, (1.2d) and for wires taken from ropes $N = 34,000$, (1.2a). As an additional test result Briem (2000) found a 19% smaller endurance for zinc-coated wires than for bright wires.

The endurance of the wires depends on the size effects of the two parameters, the wire diameter and the wire length where the wire is stressed (bending length or stressing length). The wire diameter cannot change in isolation. That means, with the wire diameter, the other parameters which influence endurance will always also be changed. Therefore, to find out the influence of the wire diameter, the other parameters which influence wire endurance should be kept as similar as possible and there should be a wide range of different wire diameters. As already mentioned, the influence of the wire diameter on the wire fatigue endurance is only known in a first form using the given results represented by equations (1.2b) and (1.2c).
The influence on wire endurance of the wire length, which is the other parameter affecting the size, can be evaluated reliably by conducting tests with parts of one and the same wire and theoretically with the help of the reliability theory. A series of wire fatigue tests done by bending over one sheave have been used to evaluate the influence of the bending length, Feyrer (1981). The wire diameter is $\delta = 0.75 \text{ mm}$, the measured tensile strength is $R_m = 1,701 \text{ N/mm}^2$. The wire bending diameter over the sheave is 115.75 mm; with these conditions the wire bending stress is $\sigma_b = 1,270 \text{ N/mm}^2$. The constant tensile stress from a loaded weight is $\sigma_{r,m} = 400 \text{ N/mm}^2$. For the test bending over one sheave, the wire is loaded by the middle stress $\sigma_m = \sigma_{r,m} + \sigma_b/2 = 1,035 \text{ N/mm}^2$ and the stress amplitude $\sigma_a = \sigma_b/2 = 635 \text{ N/mm}^2$.

The test results are shown in Fig. 1.13. Together with the points taken from the test results, the figure shows the curves calculated for the mean number of bending cycles $\bar{N}$ and the limiting number of bending cycles for 10 and 90% probability. The calculation of these curves is based on the reliability theory.

The survival probability is the smaller the larger the bending length $l$ (as a string of bending lengths $l_0$) of the wire being considered is. For a given survival probability $R_0$ of the wire bending length $l_0$, the survival probability $R(l)$ of the wire with the bending length $l$ is

$$R(l) = R_0(l-\Delta l)/(l_0-\Delta l).$$

The bending lengths $l$ and $l_0$ are the theoretical lengths without considering the bending stiffness of the wire. These lengths would occur for bending limp yarn. For the wire near the sheave, the fluctuating bending stress is small. The short bending length $\Delta l$ is introduced to take this into account. $\Delta l$ is the shorter part of the bending length having the smaller radius difference of the rope curvature than 90% of the total one. The curves in Fig. 1.13 are calculated

![Fig. 1.13. Number of bending cycles of a wire with different bending lengths, Feyrer (1981)](image-url)
using standard deviation $\lg s = 0.086$ of the logarithm normal distribution
derived from the 13 bending cycles found for the wire bending length $l_0 = 2 \times 96 \text{ mm}$. More information on this method of calculation is presented for wire
ropes in Sect. 3.2.2 where the influence of the bending length is of practical
interest.

In principle, the findings of Benjin Luo’s (2002) tensile fatigue tests pro-
duced the same result. For his tests with different stressing lengths, he used a
wire with diameter $\delta = 2 \text{ mm}$, made of material X5CrNi18-10, No. 4301 and
having tensile strength $R_m = 840 \text{ N/mm}^2$. He did 60 tensile fatigue tests for
each of the wire lengths $l = 25, 125$ and $250 \text{ mm}$ with the middle stress $\sigma_{t,m} = 356.5 \text{ N/mm}^2$ and the stress amplitude $\sigma_{t,a} = \pm 290 \text{ N/mm}^2$ only a little above
the infinite tensile fatigue strength. For the short wire length of $25 \text{ mm}$ there
are five run-outs with more than $N = 2 \times 10^6$. For the wire length $l = 250 \text{ mm}$,
the parameters for the logarithm normal distribution are the mean number of
tensile cycles $\bar{N} = 238,000$ and the standard deviation $\lg s = 0.136$.

Infinite Wire Endurance

The fatigue strengths (infinite life fatigue strengths) have been evaluated using
Wöhler-diagrams. As before, the fatigue strengths are characterized by indices
in capital letters and the stresses by indices with small letters.

For his tensile fatigue tests, Unterberg (1967) used short wire pieces with
a length between 15 and 35 mm so that he could start – without the risk
of buckling – with the middle stress $\sigma_m = 0$. The test results are shown in
Fig. 1.14. The mean relative tensile strength amplitude is

$$
\bar{\sigma}_{t,A} \left( \bar{R}_0 = 1,770; \bar{\delta} = 2.7 \right) = 0.313 \cdot R_m - 0.249 \cdot \sigma_{t,m}
$$

(1.3)

and related to the lower stress $\sigma_{t,lower}$

![Fig. 1.14. Tensile strength amplitude for wires with diameters $\delta = 1.17-4.2 \text{ mm}$ and nominal tensile strength $R_0 = 1570-1960 \text{ N/mm}^2$, Unterberg (1967)](image-url)
The standard deviation is large. As a lower limit for this tensile strength amplitude Unterberg gave the Goodman-line

$$\sigma_{t,A,\min}(R_0 = 1,770; \delta = 2.7) = 0.2 \cdot R_m - 0.2 \cdot \sigma_{t,m}.$$  

From his reverse bending tests, Unterberg (1967) found the mean relative bending strength amplitude

$$\bar{\sigma}_{b,A}(R_0 = 1,770; \delta = 2.7) = 0.27 \cdot R_m - 0.17 \cdot \sigma_{t,m}.$$ (1.3a)

The bending strength amplitude, (1.3a), is a little smaller than the tensile strength amplitude, (1.3). The deviation of the bending strength is also a little smaller than that of the tension strength to be seen in Fig. 1.14. The bending length $l = 80 \text{ mm}$ in relation to the smaller tensile stressing length $l = 15\text{–}35 \text{ mm}$ in case of tensile fatigue tests may be the reason for that. For the middle stress $\sigma_m = 0$ and the tensile strength $R_m = 1,770 \text{ N/mm}^2$, the mean bending strength amplitude (alternate bending amplitude) is $\bar{\sigma}_{b,\text{Alt}} = 0.27 \cdot R_m = 480 \text{ N/mm}^2$ and the mean tensile strength amplitude is $\bar{\sigma}_{t,\text{Alt}} = 0.31 \cdot R_m = 554 \text{ N/mm}^2$.

In any case, if the theory of stress gradient effect is valid, there should be an advantage for the bending strength. However there is no such advantage to be found in the test results. According to the theory of stress gradient effect, Faulhaber (1933), Hempel (1957) and Siebel (1959), the fatigue strength of the wire should be the greater, the greater the stress gradient in the wire cross-section is. The theory of stress gradient means that if the stress gradient is large, the outer highly stressed lay can be supported by the less stressed layer below. However the bending strength amplitude according to (1.3a) is not at all greater than the tensile strength amplitude according to (1.3) although there the stress gradient is 0. Because of this and also as a result of other observations, Unterberg (1967) stated that the theory of stress gradient does not exist for rope wires.

In Fig. 1.15 the influence of the wire diameter $\delta$ is shown using the results from different authors. In this figure the mean repetitive fatigue strength $\bar{\sigma}_{t,\text{Rep}} = 2 \cdot \bar{\sigma}_{t,A}$ is used. As a reminder, repetitive strength means that the middle stress is $\sigma_m = \sigma_{t,A}$ and the lower stress is 0. As an equation using the results in Fig. 1.15, the repetitive strength is expressed as

$$\sigma_{t,\text{Rep}} = 2 \cdot \sigma_{t,A} (\sigma_{\text{lower}} = 0) = 1,200 \cdot e^{-0.12 \cdot \delta}. \quad (1.3b)$$

The influence of the other size parameter, the stressed wire length $l$, can be evaluated for the fatigue strength amplitude in the same way as for a number of load cycles $N$ if the standard deviation of the fatigue strength amplitude for one and the same wire were known.

The influence of the tensile strength $R_m$ on the rotary bending strength $\sigma_{\text{Rot}}$ is shown in Fig. 1.16 from Wolf (1987). In this diagram, Wolf put in the results gained by Buchholz (1965) wires with lower tensile strength to get an
overview for a greater strength range. For small tensile strengths, the rotary bending strength increases almost proportionally with tensile strength $R_m$. The rotary bending strength does not increase as much for rope wires (wires with tensile strength between 1,300 and 2,200 N/mm$^2$). According to Wolf (1987), it is

$$\sigma_{\text{Rot}} = 0.334 + 0.173 \cdot R_m.$$  \hfill (1.3c)

That means that with increasing tensile strength $R_m$, the relative rotary bending strength $\sigma_{\text{Rot}}/R_m$ will be reduced as seen in Fig. 1.17, Wolf (1987).

Ziegler, Vogel and Wehking (2005) and Wehking (2005) evaluated the rotary bending strength from tests with the Stuttgart rotary bending machine to be

$$\lg \sigma_{\text{Rot}} = 1.411 + 0.396 \cdot \lg R_m - 0.128 \cdot \lg \delta.$$  \hfill (1.3d)

According to (1.3d), the rotary bending strength for new wires with tensile strength $R_m = 1,770$ N/mm$^2$ and wire diameter $\delta = 1$ mm is $\sigma_{\text{Rot}} = 500$ N/mm$^2$. According to (1.3c), Wolf (1987) found the mean rotary bending strength for different wires to be between $\sigma_{\text{Rot}} = 510$ N/mm$^2$ and 730 N/mm$^2$ for wires with diameters between 0.8 and 1.0 mm taken from wire ropes and tested under the same conditions.

The fatigue strength is reduced for wires with zinc coating, Reemsnyder (1969), and especially for wires with a thick zinc coating, Apel and Nüninghoff

---

**Fig. 1.15.** Repetitive tensile strength for different wire diameters $\delta$ for a mean nominal tensile strength $R_0 = 1,720$ N/mm$^2$
Fig. 1.16. Alternate strength $\sigma_{\text{Alt}}$ for wires with a great range of measured tensile strength $R_m$, Wolf (1987)

Fig. 1.17. Relative rotary bending strength $\sigma_{\text{Rot}}/R_m$ for rope wires, Wolf (1987)

(1979). For normal zinc-coated wires, Briem (2000) also found that fatigue endurance is reduced in relation to bright wires. On the other hand, the corrosion that should be prevented by the zinc coating. Corrosion reduces the fatigue strength enormously, as can be seen in Fig.1.18, Jehnlich (1969).

The fatigue strength of wires depends on their various contents and method of manufacture. With the loss of cross-section during repeated wire drawing, the repetitive tensile strength $\sigma_{t,\text{Rep}}$ first increases and then decreases. The