LATENT CLASS AND LATENT TRANSITION ANALYSIS
LATENT CLASS AND LATENT TRANSITION ANALYSIS

With Applications in the Social, Behavioral, and Health Sciences

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For David and Kathy
with admiration
(LMC)

For Dad
my first math teacher
(STL)
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