

MIXED NUMBERS

$$\frac{\text{Number of dose}}{\text{Number of days}} \times X \text{ kg} = 66 \text{ lb} \times \frac{1 \text{ kg}}{2.2 \text{ lb}}$$

DOSAGE CALCULATION

# Medical Mathematics and Dosage Calculations

## for Veterinary Professionals

SECOND EDITION

**Robert Bill**

$$\frac{V1 \times C1}{V2} = C2$$

FRACTIONS

$$100 \times 35 \times \frac{1}{50} = 50 \times \frac{1}{50} \times X$$

INTRAVENOUS INFUSION

$$\frac{20}{5} \times X = 2 \times \frac{3}{1}$$

$$X \text{ mL} = \text{Drips (gtt)} \times \text{IV set calibration}$$

DOSE RANGES

$$\frac{V1 \times C1}{100 \text{ mL}} = \frac{V2 \times C2}{X \text{ mL}}$$

SYRINGE UNITS OF MEASUREMENT

$$\frac{\text{Unknown } X \text{ unit}}{\text{Known value unit}} = \frac{\text{Conversion factor with } 10 \text{ grains}}{\text{Conversion factor with } 0.5 \text{ gtt}}$$

**MEDICAL  
MATHEMATICS  
AND  
DOSAGE  
CALCULATIONS**



**FOR VETERINARY  
PROFESSIONALS**

Second Edition



# **MEDICAL MATHEMATICS AND DOSAGE CALCULATIONS**



**FOR VETERINARY  
PROFESSIONALS**

**Second Edition**

**ROBERT BILL, DVM, MS, PhD**



**WILEY-BLACKWELL**

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## SELF-ASSESSMENT

**Objectives**

1. Conduct a self-assessment.
2. Identify areas needed for review.

In a medical situation, the most beneficial drug can be rendered worthless or dangerous if the veterinarian or veterinary technician does not accurately calculate the dose. As many veterinary professionals can testify, it is not enough to have a superficial understanding of dosage calculation because superficial knowledge often fails in the crisis situation of an emergency. Therefore, it is important that veterinary professionals have the basics of dose and dosage calculation firmly entrenched in their working memory.

Learning theory and common sense tell us that any mental activity practiced on a routine basis becomes second nature. It is important that the veterinary professional practice these routine dosage calculation procedures on a regular basis in order to ensure greatest accuracy whenever a dose for a patient needs to be administered.

Another obligation of professionals is to accurately define the limits of their knowledge and to strengthen the weaker areas of their

skills or knowledge. To help you define the areas of math and dosage calculation that you need to refresh or review, complete the following self-assessment exercises.

For those sections of the self-assessment that you identify as areas where a review would be useful, work through the chapters and sections of the book to which that section of the self-assessment exercise refers.

### **SELF-ASSESSMENT EXERCISE**

1. Add or subtract the following decimal numbers:

a)  $1.5 + 2 =$

b)  $1.9 + 9.7 =$

c)  $4.55 + 7.43 =$

d)  $0.52 + 0.09 =$

e)  $0.003 + 1.0 =$

f)  $5.5 - 2.5 =$

g)  $6.0 - 3.9 =$

h)  $13.125 - 1.50 =$

i)  $0.251 - 0.095 =$

j)  $0.00252 - 0.0009 =$

2. Multiply or divide the following decimal numbers:

a)  $5 \times 2.5 =$

b)  $3.0 \times 8.35 =$

c)  $24.75 \times 12.35 =$

d)  $0.02 \times 15.5 =$

e)  $0.003 \times 0.0125 =$

f)  $15 \div 2.5 =$

g)  $2.5 \div 1.5 =$

h)  $35 \div 0.5 =$

i)  $0.25 \div 0.125 =$

j)  $0.010 \div 0.0025 =$

3. Round the following decimal numbers to the nearest  $1/100$  and the nearest  $1/10$ :

a)  $10.594 =$

b)  $4.682 =$

c)  $1.233 =$



d)  $9.452 =$

e)  $23.675 =$

4. Simplify the following fractions to their lowest form (e.g.,  $6/8 = 3/4$ ):

a)  $\frac{2}{10} =$

b)  $\frac{4}{16} =$

c)  $\frac{3}{12} =$

d)  $1\frac{6}{8} =$

e)  $5\frac{4}{32} =$

5. Add or subtract the following fractions:

a)  $\frac{3}{4} + \frac{1}{4} =$

b)  $\frac{1}{16} + \frac{3}{32} =$

c)  $\frac{2}{5} + \frac{1}{6} =$

d)  $1\frac{1}{2} + 2\frac{3}{4} =$

e)  $4\frac{2}{3} + 5\frac{7}{8} =$

f)  $\frac{1}{2} - \frac{1}{4} =$

g)  $\frac{2}{3} - \frac{1}{6} =$

h)  $1\frac{3}{4} - \frac{7}{8} =$

i)  $3\frac{15}{16} - 2\frac{3}{8} =$

j)  $45\frac{1}{5} - 33\frac{7}{8} =$

6. Multiply the following fractions:

a)  $\frac{1}{2} \times \frac{1}{2} =$

b)  $\frac{3}{4} \times \frac{1}{2} =$

c)  $\frac{3}{4} \times \frac{12}{16} =$

d)  $\frac{7}{8} \times 1\frac{1}{2} =$

e)  $\frac{11}{16} \times \frac{3}{4} =$

f)  $2\frac{3}{4} \times 4\frac{1}{2} =$

g)  $5\frac{4}{7} \times 1\frac{3}{4} =$

h)  $10\frac{3}{8} \times 9\frac{1}{3} =$

7. Divide the following fractions:

a)  $\frac{1}{2} \div \frac{1}{4} =$

b)  $2\frac{1}{2} \div \frac{1}{2} =$

c)  $3\frac{3}{4} \div \frac{1}{16} =$

d)  $22\frac{4}{8} \div \frac{2}{32} =$

e)  $125\frac{1}{5} \div \frac{4}{25} =$

8. Convert the following fractions to decimal numbers (e.g.,  $1/2 = 0.5$ ):

a)  $\frac{2}{10} =$

b)  $\frac{14}{28} =$

c)  $\frac{3}{21} =$

d)  $1\frac{1}{2} =$

e)  $4\frac{5}{6} =$

f)  $15\frac{7}{16} =$

9. Convert the following decimal numbers to the common fraction (e.g.,  $0.5 = 1/2$ ):

a)  $0.25 =$

b)  $0.333 =$

c)  $0.75 =$

d)  $0.125 =$

e)  $1.5 =$

f)  $2.500 =$

10. Convert the following percentages to decimal numbers:

a)  $25\% =$

b)  $79\% =$

c)  $100\% =$

d)  $6\% =$

e)  $0.2\% =$

f)  $0.0087\% =$

11. Convert the following decimal numbers to percentages:

a)  $0.5 =$

b)  $0.45 =$

c)  $1.00 =$

d)  $0.103 =$

e)  $0.90023 =$

12. Convert the following percentages to commonly used fractions (e.g.,  $50\% = 1/2$ ):

a)  $25\% =$

b)  $75\% =$

c)  $33.3\% =$

d)  $10\% =$

e)  $80\% =$

13. Convert the following fractions to percentages (e.g.,  $1/2 = 50\%$ ):

a)  $\frac{3}{4} =$

b)  $\frac{8}{10} =$

c)  $\frac{15}{45} =$

d)  $\frac{10}{10} =$

e)  $\frac{1}{1000} =$