# Shaoyuan Li • Yi Zheng

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Shaoyuan Li and Yi Zheng

Shanghai Jiao Tong University, China

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### Preface

There is a class of complex plant-wide systems which are composed of many physically or geographically divided subsystems. Each subsystem interacts with some so-called neighboring subsystems by their states and inputs. The technical target is to achieve a specific global performance of the entire system.

The classical centralized control solution, which could obtain a good global performance, is often impractical for application to a plant-wide system for computational reasons and lack of error tolerance. When the centralized controller fails or a control component fails, the entire system is out of control and the control integrity cannot be guaranteed.

The distributed (or decentralized) framework, where each subsystem is controlled by an independent controller, has the advantages of error-tolerance, less computational effort, and flexibility to system structure. Thus the distributed control framework is usually adopted in this class of system, in spite of the fact that the dynamic performance of centralized framework is better. Thus, how to improve the global performance under distributed control framework is a valuable problem.

Model predictive control (MPC), as a highly practical control technology with high performance, has been successfully applied to various linear and nonlinear systems in the process industries, and is becoming more widespread. The distributed framework of MPC, distributed MPC (DMPC), is also gradually developed with the development of communication network technologies in process industries that allow the control technologies and methodologies to utilize their potentials for improving control.

For the MPC algorithm applied to the plant-wide systems, the system's architectures can be divided as follows:

- 1. Centralized MPC, which is a MIMO system architecture;
- 2. Decentralized MPC, one controller-one subsystem, but no information exchange between controllers, and
- Distributed MPC, which assumes that each subsystem can exchange information with its neighbor's subset of other subsystems.

Since the centralized MPC is forbidden for the large-scale plant-wide system with hundreds (or thousands) of inputs and outputs variables due to its lesser flexibility, weak error tolerance and the large cost of computation, the distributed framework is usually adopted despite its lower global performance. The schematic of distributed MPC is shown in Figure 1, the whole system is composed by many spatial distributed interconnected sub-systems. Each



Figure 1 The schematic of distributed model predictive control

subsystem is controlled by a subsystem-based MPC and these controllers are interconnected by the network.

As mentioned before, how to improve the global performance under distributed control framework is a valuable problem. It is exactly true for the DMPC. There are many DMPC strategies and design methods in the literature, all to different ends. We have done extensive research in this topic for more than 10 years, and have proposed some strategies, e.g., the Nash optimization-based DMPC and the impacted region optimization based DMPC, etc. We found that the DMPC is definitely a useful method for large-scale plant-wide systems. Thus, we decided to write this book.

This book systematically introduces different distributed predictive control methods for plant-wide systems, including system decomposition, classification of distributed predictive control, unconstrained distributed predictive control, and the stabilized distributed predictive control with different coordinating strategies for different purposes, as well as the implementation examples of distributed predictive control. The major new contribution of this book is to show how the distributed MPCs can be coordinated efficiently for different control requirements, namely network connectivity, error tolerance, performance of entire closed-loop system, calculation speed, etc., and how to design distributed MPC. The remaining contents of this book are structured into four parts.

In the first part, we recall the main concepts and some fundamental results of the predictive control for discrete-time linear systems. The system structure model and some decomposition methods to present how to divide the entire system into interacting subsystems according to the specific control requirements is also introduced. Our intent is to provide the necessary background knowledge to understand the rest of the book.

The second part introduces the unconstrained distributed MPCs with different coordination strategies. The simplest and most practical local cost optimization based distributed MPC, Nash optimization based distributed MPC, the cooperative distributed MPC that can obtain very good performance of the entire system but each subsystem-based MPC of which requires

the information of the whole system, and the networked distributed MPC with information constraints, which is a tradeoff between the two methods mentioned above. For primary readers, the major ideas and characteristics of distributed MPCs are clearly explained in a simple way without constraints.

The third part focuses on introducing the design of the stabilizing distributed MPCs with constraints for the three types of DMPCs: the local cost optimization based DMPC, the cooperative DMPC, and the networked DMPC with information constraint, respectively. The designed DMPCs can guarantee recursive feasibility and the asymptotic stability of the closed-loop system if the initial feasible solution exists.

In the last part, three practical examples are given to illustrate how to implement the introduced distributed MPC into industrial processes, they are the nonlinear networked DMPC for accelerated cooling processes in heavy plate steel mills, the speed train control with unconstrained networked DMPC, and the hierarchical DMPC for load control of a high building with multicooling resources.

In conclusion, this book tries to give a systematic overview of the latest distributed predictive control technologies to readers. We hope this book can help engineers to design control systems in their daily work or in their new projects. In addition, we believe that this book is fit for the graduate students who are pursuing their master or doctor degree in control theory and control engineering. We will be very pleased if this book is of use to you if you are interested in the control of plant-wide systems or predictive control.

Shaoyuan Li Yi Zheng

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# 1

### Introduction

### 1.1 Plant-Wide System

There is a class of systems which are composed of many interacted subsystems' industrial fields. Especially with the development of the advanced technology and the increase in the requirement of products, many new distributed processes have appeared, the processes of producing products have become more and more complex, and the scales of industrial processes have become more and more large. The automation structure for this kind of systems has changed from the traditional centralized automation system to a decentralized and centralized automation system.

Correspondingly, the control algorithm and control structure for this kind of system change from centralized control and decentralized control to the distributed control system. The distributed control refers to a control system where each subsystem is controlled by an individual controller, and these controllers communicate with other subsystem-based controllers and are coordinated according to the exchanged information for obtaining good global performance or some special common goals. So far, the distributed control, especially the DMPC, has been studied and are still being studied by many scientists, and many theories and algorithms have been developed. We think it is the right time to introduce the distributed control to more students and engineers.

To make it more clear which kind of system is suitable for distributed control, we give some examples as follows.

#### 1. Wind power generation farm

In a wind turbine power generation farm, as shown in Figure 1.1, wind turbines are spatially distributed. The output wind flow rate of each wind turbine decreases with increasing generated power. It affects the input wind flow rate of the downstream wind turbines, and then their dynamics. In this way, these wind turbines interact with each other. For the automation system, each wind turbine is controlled by an individual controller. And these controllers are connected by a network (fieldbus) and are able to communicate with each other by the network.

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Figure 1.1 The wind farm

#### 2. Multizone building temperature regulation system

Multizone building temperature regulation systems are a class of typical spatially distributed systems, as shown in Figure 1.2, which are composed of many physically interacted subsystems (rooms or zones) labeled as  $S_1, S_2, \ldots, S_m$ , respectively. The thermal influences between rooms of the same building occur through internal walls (the internal walls' isolation is weak) and/or door openings. A thermal meter and a heater (or air conditioner) are installed in each zone, which is used to measure and adjust the temperature of the multizone building.

#### 3. Distributed power network

Power networks are large networks consisting of a large number of components. The dynamics of the power network as a whole are the result of interactions between the individual components. The generators produce power that is injected into the network on the one side, while the loads consume power from the network on the other. If we consider each power plant, load, and station as a subsystem, it is a typical distributed system, whose subsystems interacted with each other and controlled separately.

In addition, since the number of players involved in the generation and distribution of power has increased significantly, in the near future, the number of source nodes of the power distribution network will increase even further as large-scale industrial suppliers and small-scale individual household will also start to feed electricity into the network. As a consequence, the structure of the power distribution network will change into a much more decentralized system with many generating sources and distribution agencies (Figure 1.3).



Figure 1.2 The multizone building temperature regulation system



Figure 1.3 Distributed power generation power network

### 1.2 Control System Structure of the Plant-Wide System

The control structure is a very general concept. It includes how to schedule the controllers, and the inputs/outputs of each controller. The control system structure of the plant-wide system is shown in Figure 1.4, which is a hierarchical structure. The top layer, denoted as layer 4, is a steady economic optimization layer which is used to optimize the key process parameters, e.g., the product quantity, product quality, feeding material quality, etc. Layer 3 is a real-time optimization layer which dynamically optimizes the set-point of the multivariable layers.



Figure 1.4 Hierarchical control system for the plant-wide system

This layer considers the dynamic economic performance and efficiency. The slow time variation of the process condition is taken into account in this layer. Below this layer is a multivariable layer which coordinates the interaction between each control loop and gives a set-point for the field control loop. The lowest layer, a field control loop layer, which is not drawn in this figure, is used to regulate the process variable, e.g., the temperature, flow rate, or pressure. In some cases, the multivariable takes some work of the field control loop layer when the control problem is complicated. In this structure, with an increase in the layer level, the information to communicate is deduced, and the computing interval is increased.

Here, we consider the multivariable control layer. For a plant-wide system, there are many inputs and outputs. With the development of a network, communication technology, and fieldbus product, as well as intelligent meters, the control theory for a multivariable system is developed correspondingly. Many advanced control methods appear in the literature works, and the control structure in a multivariable layer changes from the centralized control to the decentralized control, to the distributed control. In addition, recently, the distributed structures for the real-time dynamic optimization layer and steady-state optimization layer have also appeared in the literature works. The real-time optimization layer and multivariable control loop are combined together in some cases. This is out of the scope of discussion in this book. In the following, three types of control structures, centralized control structure, decentralized control structure, and distributed control structure, in a multivariable control layer are specified to show the advantage of the distributed control framework.

#### 1.2.1 Centralized Control

As shown in Figure 1.5, the centralized multivariable controller gets all the information of the plant-wide system, and then calculates the control law of all the inputs together, and sends the