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Sujay Kumar Dutta
Dharmesh R. Lodhari

Extraction of Nuclear and Non-ferrous Metals

 Springer

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Extraction of Nuclear and Non-ferrous Metals

 Springer

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Preface

Extraction of Nuclear and Non-Ferrous Metals is a basic science and has a wide applicability in extraction and refining of metals. This book covers the undergraduate curriculum in **Nuclear Metallurgy and Extraction of Non-Ferrous Metals** as prescribed for degree courses and allied professional courses in Metallurgical and Materials Engineering.

Chapter 1 of this textbook, *Fundamentals of Nuclear Metallurgy*, covers almost all the important basic concepts of **Nuclear Metallurgy** for graduate engineering students. Even postgraduate students, engineers and researchers can brush up their understanding. Chapters 2–6 briefly cover **Nuclear Metals**, their extraction, properties and applications.

Chapters 7–13 discuss **Extractive Metallurgy of Common Metals**. There are detailed discussions about production of common metals (like copper, aluminium, zinc, lead etc.), their properties and applications.

Chapters 14–20 describe the **Extractive Metallurgy of Less Common/Ferro-Alloying Metals**. Their production, properties and applications are discussed in detail. Chapter 21 discusses **Ultra-High-Purity Metals Production**.

Needless to say that although few books are available, none discusses the subject matter of **Nuclear Extractive Metallurgy** in easily understood terms for students. Based on our experience of teaching this subject at undergraduate level for more than three decades, we have made a sincere attempt to cover the topics of **Nuclear Metallurgy** in an easy way.

In spite of taking all possible care, there may be some errors or mistakes left unnoticed. If so, please feel free to interact with us. We poured our long experience into this project, and also collected the information from several sources. We are indebted to one and all, from whose valuable knowledge we have been benefited. Thanks all of them.

We are confident that this textbook will make the subject matter of *Extraction of Nuclear and Non-Ferrous Metals* more simple and easy to understand. We wish to thank the publisher Springer for their continuous support in preparation and publication of this textbook within a short period.

Vadodara, India

Sujay Kumar Dutta
Dharmesh R. Lodhari

Contents

Part I Extractive Metallurgy of Nuclear Metals

1	Fundamentals of Nuclear Metallurgy	3
1.1	Atomic Structure.....	3
1.2	Isotopes.....	4
1.3	Nuclear Binding Energy.....	4
1.4	Radioactivity.....	6
1.5	Rate of Radioactive Decay.....	8
1.6	Neutron Reaction.....	9
1.7	Cross-Sections for Neutron Reactions.....	12
1.8	Multiplication Factors.....	12
1.9	Types of Reactor.....	13
1.10	Nuclear Fuel and Breeding Reaction.....	14
1.11	Cladding Materials.....	16
1.12	Radiation Damage.....	16
	1.12.1 Atomic Displacement.....	17
	1.12.2 Temperature Spikes.....	18
	1.12.3 Physical Effects of Radiation.....	18
1.13	Reprocessing of Irradiated Fuel.....	19
	1.13.1 Cooling Irradiated Fuel Elements.....	20
	1.13.2 Head-End Processes.....	21
	1.13.3 Separations or Extraction Process.....	21
1.14	Processing of Nuclear Metals.....	22
	1.14.1 Separation Processes.....	24
	1.14.2 Extraction Techniques.....	25
2	Uranium	27
2.1	Introduction.....	27
2.2	Sources.....	28
2.3	Extraction of Uranium from Ore.....	29

2.3.1	Acid Leaching	29
2.3.2	Ion Exchange Separation	29
2.3.3	Production of Reactor Grade Uranyl Nitrate	32
2.3.4	Production of Uranium Dioxide	32
2.3.5	Reduction of Uranium Compounds	33
2.3.6	High Purity Uranium Metal	35
2.4	Properties	35
2.5	Applications	37
3	Plutonium	39
3.1	Introduction	39
3.2	Sources	40
3.3	Extraction of Plutonium	41
3.3.1	Separation of Plutonium	41
3.3.2	Reduction to Plutonium Metal	47
3.3.3	Extraction of Plutonium from Spent Fuel	48
3.4	Properties	48
3.5	Applications	50
4	Zirconium	53
4.1	Introduction	53
4.2	Sources	53
4.3	Extraction of Zirconium	54
4.3.1	Separation of Zirconium and Hafnium	54
4.3.2	Preparation of Zirconium Oxide	57
4.3.3	Production of Zirconium Tetrachloride	57
4.3.4	Reduction of $ZrCl_4$ by Mg or Na	57
4.4	Properties	59
4.5	Applications	60
5	Hafnium	63
5.1	Introduction	63
5.2	Sources	63
5.3	Extraction of Hafnium	64
5.3.1	Separation of Zirconium and Hafnium	64
5.3.2	Preparation of HfO_2	64
5.3.3	Production of Hafnium Metal	64
5.4	Properties	66
5.5	Applications	67
6	Thorium	69
6.1	Introduction	69
6.2	Sources	70
6.3	Extraction of Thorium	70
6.3.1	Separation of Thorium Compound from Monazite	70

6.3.2	Thorium Oxalate Formation	74
6.3.3	Chlorination of Thorium Oxalate	74
6.3.4	Purification of ThCl_4	75
6.3.5	Reduction of ThCl_4	75
6.3.6	Purification of Thorium Metal	76
6.4	Production of Thorium Powder	76
6.5	Production of Massive Thorium Metal	77
6.6	Properties	78
6.7	Applications	79

Part II Extractive Metallurgy of Common Metals

7	Copper	85
7.1	Introduction	85
7.2	Sources	85
7.3	Extraction of Copper	86
7.3.1	Concentration	86
7.3.2	Roasting	86
7.3.3	Smelting	88
7.3.4	Converting	90
7.3.5	Refining	93
7.4	Newer Processes	96
7.4.1	Flash Smelting Process	98
7.4.2	Continuous Process	99
7.5	TORCO Segregation Process	102
7.6	Recovery of Precious Metals	103
7.7	Hydrometallurgical Process of Copper	105
7.7.1	Ferric Chloride Leaching	105
7.7.2	Leaching of Low Grade Ores	105
7.7.3	Leaching of Roasted Sulphide Concentrates	106
7.8	Properties	107
7.9	Applications	109
8	Aluminium	111
8.1	Introduction	111
8.2	Sources	111
8.3	Extraction of Aluminium	112
8.3.1	Bayer Process	112
8.3.2	Hall-Heroult Process	115
8.3.3	Refining of Aluminium	121
8.4	Properties	122
8.5	Applications	123

9	Zinc	125
9.1	Introduction	125
9.2	Sources	125
9.3	Extraction of Zinc	126
9.3.1	Pyrometallurgical Process	126
9.3.2	Hydrometallurgical Process	132
9.4	Properties	134
9.5	Applications	134
10	Lead	137
10.1	Introduction	137
10.2	Sources	137
10.3	Extraction of Lead	138
10.3.1	Concentration	139
10.3.2	Dead Roasting	139
10.3.3	Smelting	140
10.3.4	Refining	143
10.4	Properties	146
10.5	Applications	146
11	Tin	149
11.1	Introduction	149
11.2	Sources	149
11.3	Extraction of Tin	149
11.3.1	Concentration	150
11.3.2	Reduction of Concentrate	151
11.3.3	Treatments of Slags for Recovery of Metals	151
11.3.4	Refining	152
11.4	Properties	153
11.5	Applications	154
12	Magnesium	155
12.1	Introduction	155
12.2	Sources	155
12.3	Extraction of Magnesium	156
12.3.1	Pyrometallurgical Process	157
12.3.2	Electrometallurgical Process	161
12.3.3	Other Processes for Extraction of Mg	165
12.4	Properties	165
12.5	Applications	165
13	Nickel	167
13.1	Introduction	167
13.2	Sources	167
13.3	Extraction of Nickel	168

13.3.1	Concentration	168
13.3.2	Treatment of Ni–Cu Sulphide Concentrate	169
13.3.3	Refining	170
13.4	Properties	173
13.5	Applications	174

Part III Extractive Metallurgy of Less Common Metals and Ferro-Alloying Metals

14	Silicon	179
14.1	Introduction	179
14.2	Sources	179
14.3	Extraction	180
14.3.1	Metallic Silicon	180
14.3.2	Ferro-Silicon	181
14.4	Properties	183
14.5	Applications	183
15	Manganese	185
15.1	Introduction	185
15.2	Sources	185
15.3	Extraction	186
15.3.1	Beneficiation	186
15.3.2	Metallic Manganese	186
15.3.3	Ferro-Manganese	187
15.4	Properties	189
15.5	Applications	190
16	Chromium	193
16.1	Introduction	193
16.2	Sources	193
16.3	Extraction	194
16.3.1	Metallic Chromium	194
16.3.2	Ferro-Chromium	195
16.4	Properties	198
16.5	Applications	198
17	Tungsten	201
17.1	Introduction	201
17.2	Sources	201
17.3	Extraction	202
17.3.1	Metallic Tungsten	202
17.3.2	Ferro Tungsten	203
17.4	Properties	203
17.5	Application	204

18	Molybdenum	205
18.1	Introduction	205
18.2	Sources	205
18.3	Extraction	206
18.3.1	Concentration of Molybdenite	206
18.3.2	Metallic Molybdenum	207
18.3.3	Calcium Molybdate	208
18.3.4	Ferro-Molybdenum	208
18.4	Properties	209
18.5	Applications	209
19	Vanadium	211
19.1	Introduction	211
19.2	Sources	211
19.3	Extraction	212
19.3.1	Recovery of Vanadium Pentoxide	212
19.3.2	Metallic Vanadium	212
19.3.3	Ferro-Vanadium	215
19.4	Properties	217
19.5	Applications	218
20	Niobium and Tantalum	219
20.1	Introduction	219
20.2	Sources	219
20.3	Extraction	220
20.3.1	Separation of Niobium and Tantalum from Ores	220
20.3.2	Metallic Niobium	220
20.3.3	Metallic Tantalum	223
20.3.4	Ferro-Niobium	225
20.4	Properties	226
20.4.1	Niobium	226
20.4.2	Tantalum	226
20.5	Applications	227
20.5.1	Niobium	227
20.5.2	Tantalum	228

Part IV Production of Ultra-High Purity Metals

21	Methods of Refining	231
21.1	Introduction	231
21.2	Zone Refining	231
21.3	Vacuum Induction Melting	233
21.4	Vacuum Arc Melting	234
21.5	Inert Atmosphere Arc Melting	237
21.6	Electron Beam Melting	238

Contents	xiii
Appendix	243
Some Thermodynamic Data*	245
Bibliography	247

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Professor Dutta has published three books along with other authors: *Metallurgical Thermodynamics, Kinetics and Numericals* (2011); *Alternate Methods of Ironmaking (Direct Reduction and Smelting Reduction Processes)* (2012); *Iron Ore–Coal/Coke Composite Pellets* (2013), and *Extractive Metallurgy (Processes and Applications)* is currently in publication. He has also published 120 papers in national and international journals and conference proceedings.

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Part I
Extractive Metallurgy of Nuclear Metals

Chapter 1

Fundamentals of Nuclear Metallurgy

1.1 Atomic Structure

The operation of a nuclear reactor depends upon various interactions of neutrons with atomic nuclei. In order to understand the nature and characteristics of these reactions, it is desirable to consider briefly some of the fundamentals of atomic and nuclear physics. An atom consists of a positively charged *nucleus* surrounded by a number of negatively charged *electrons*; so the atom as a whole is electrically neutral. Atomic nuclei are combination of two primary particles, namely, *protons* and *neutrons*. Protons and neutrons are jointly named nucleus. The protons carry a single unit positive charge, equal in magnitude to the electronic charge. The neutron is very slightly heavier than the proton and it is an electrically neutral particle carrying no charge. The neutrons are the heart of nuclear energy and they play an important role in the release of atomic energy. All atomic nuclei, with the exception of hydrogen, contain one or more neutrons in addition to protons.

Atomic energy is derived by virtue of the transformation of matter into energy. Calculations show that the conversion of small amount as 1 g of matter yields energy equivalent of 25 million kWh. By contrast, the combustion of the same amount of coal gives the insignificant amount of 0.0085 kWh. The difference in these figures shows the distinction between atomic and chemical energy.

For a given element, the number of protons present in the atomic nucleus is called the *atomic number* and is denoted by Z . It is similar to the number of the element in the *Periodic Table* (Fig. 1.1).

e.g. $H \rightarrow 1$, $He \rightarrow 2$, $Li \rightarrow 3$, $C \rightarrow 6$, $O \rightarrow 8$, $Fe \rightarrow 26$, $U \rightarrow 92$ etc.

The total number of protons and neutrons in an atomic nucleus is called the *mass number* of the element and is denoted by A . Hence, number of neutrons in the atomic nucleus is $(A - Z)$. In general the element (M) can be represented by ${}_Z M^A$.

The periodic table is color-coded by groups. The legend below the table identifies the colors:

- Alkali Metal: Red
- Alkaline Earth: Orange
- Transition Metal: Yellow
- Semimetal: Light Green
- Nonmetal: Green
- Basic Metal: Blue
- Halogen: Teal
- Noble Gas: Light Blue
- Lanthanide: Purple
- Actinide: Pink

Fig. 1.1 Periodic Table of the elements

1.2 Isotopes

It is the atomic number, i.e. the number of protons in the nucleus, which determines the chemical nature of an element. This is so because the chemical properties depend on the orbital electrons which are surrounding the nucleus; and their number must be equal to the number of protons, since the atom as a whole is electrically neutral.

Atoms with nuclei containing the same numbers of protons (i.e. with the same atomic number, but with different mass numbers) are essentially identical chemically, although they frequently exhibit marked differences in their nuclear characteristics. Such species, having the same atomic number but different mass numbers, are called *isotopes*. Uranium-232 (${}_{92}\text{U}^{232}$) has three isotopic forms in nature, with mass numbers 234, 235, and 238 (${}_{92}\text{U}^{234}$, ${}_{92}\text{U}^{235}$ and ${}_{92}\text{U}^{238}$).

1.3 Nuclear Binding Energy

By means of the mass spectrograph, it has been shown that the actual mass is always less than the sum of the masses of the constituent nucleus. The difference is known as *mass defect*, which is related to the energy binding of particles in the nucleus. If m_p , m_n and m_e represent the masses of the proton, neutron and electron respectively, the sum of the masses of the constituents of an atom is $Zm_p + (A - Z)m_n$. Suppose the observed mass of the atom is M , then

$$\text{mass defect} = [Z(m_p + m_e) + (A - Z)m_n] - M = Zm_H + (A - Z)m_n - M \quad (1.1)$$

where $m_p + m_e = m_H$, the mass of the hydrogen atom.

Since $m_H = 1.008145 \text{ amu}^*$ and $m_n = 1.008986 \text{ amu}$

($\text{amu}^* \rightarrow \text{atomic mass unit}$ is defined as exactly one-sixteenth of the mass of oxygen (O^{16}) atom or one-twelfth of the mass of carbon (C^{12}) atom.)

Therefore,

$$\text{mass defect} = [1.008145 Z + (A - Z) 1.008986 - M] \quad (1.2)$$

The mass defect is a measure of the energy which would be released, if the individual Z protons and $(A - Z)$ neutrons combined to form a nucleus. Conversely, it is numerically equal to the energy which would have to be supplied to break apart the nucleus into its constituents. Thus, the energy equivalent of the mass defect is called the *binding energy* of the nucleus; i.e. the energy, which holds together the nucleus of an atomic nucleus, is named the *binding energy*.

If m is the decrease in mass accompanying any particular process, then the equivalent amount of energy E released is given by the Einstein equation:

$$E = mc^2 \quad (1.3)$$

where m is mass in grams, c is velocity of light = $2.998 \times 10^{10} \text{ cm/sec}$

Therefore,

$$E = m \times 8.99 \times 10^{20} \text{ ergs} \quad (1.4)$$

In the nuclear energy, energies are usually stated in terms of the *electron volt unit*, represented by ev . Since the electronic charge is $1.602 \times 10^{-19} \text{ C}$.

$$\text{The electrical energy, } e = vQ \text{ J,} \quad (1.5)$$

where v is in volts, and Q is the amount of electricity in coulomb.

If $1 \text{ ev} = 1.602 \times 10^{-19} \text{ J} = 1.602 \times 10^{-12} \text{ erg}$ (since $1 \text{ J} = 10^7 \text{ erg}$)

1 Mev (million electron volts) = $1.602 \times 10^{-6} \text{ erg}$

Therefore,

$$\begin{aligned} E (\text{Mev}) &= m (\text{gm}) \times [(8.99 \times 10^{20}) / (1.602 \times 10^{-6})] = 5.612 \times 10^{26} m \\ &= 5.612 \times 10^{26} \times 1.66 \times 10^{-24} m = 931.59 m (\text{amu}) \end{aligned} \quad (1.6)$$

Since $1 \text{ amu} = 1.66 \times 10^{-24} \text{ gm}$

The numerical value of the nuclear binding energy in Mev can be obtained upon multiplying by 931.6, the mass defect in amu, as given by Eq. (1.2). A more useful quantity is the average binding energy per nucleon, which is equal to the total binding energy (BE) divided by the number of nucleons, i.e. by the mass number A ; hence from Eqs. (1.2) and (1.6):

$$[BE/A] = [(931.59/A) \times \{1.008145 \times Z + 1.008986 \times (A - Z) - M\}] \quad (1.7)$$

Example 1.1 Determine the binding energy per nucleon in (a) Sn-120 for which M is 119.9401 amu and (b) U-235 for which M is 235.1175 amu.

Solution: (a) The atomic number of Sn is 50, i.e. $Z = 50$ and $A = 120$
 Since $[BE/A] = [(931.59/A) \times \{1.008145 \times Z + 1.008986 \times (A - Z) - M\}]$
 Therefore,

$$\begin{aligned} [BE/A] &= [(931.59/120) \times \{(1.008145 \times 50) + (1.008986 \times 70) - 119.9401\}] \\ &= \mathbf{8.51 \text{ Mev per nucleon}} \end{aligned}$$

(b) The atomic number of U is 92, i.e. $Z = 92$ and $A = 235$

$$\begin{aligned} [BE/A] &= [(931.59/235) \times \{(1.008145 \times 92) + (1.008986 \times 143) - 235.1175\}] \\ &= \mathbf{7.59 \text{ Mev per nucleon}} \end{aligned}$$

1.4 Radioactivity

There are conventional electrostatic repulsive forces between the positively charged protons. When the atomic number is low, the repulsive force among the protons is small. Hence, the proton–proton, neutron–neutron, and proton–neutron forces are roughly equal; a neutron/proton ratio is close to unity, to be expected for stability. But with increasing atomic number, electrostatic repulsion between the protons, which varies as Z^2 , becomes more and more important. Since, the total electrostatic repulsion force between all the protons in the nucleus is proportional to the square of their number, i.e. to Z^2 .

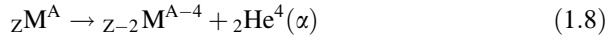
In order to maintain stability, the nuclei must now contain an increased proportion of neutrons, so that the attractive neutron–neutron and neutron–proton forces can compensate for the rapidly increasing repulsive forces between the protons. But there is a limit. Consequently, the elements of atomic number 84 or larger have no stable isotopes; although elements 84 (polonium, Po) through 92 (uranium, U) exist in nature, they are unstable and exhibit the phenomenon of *radioactivity*.

Since properties of atomic nuclei depend on the total number of protons and neutrons (nucleons) in the nucleus, isotopes of one and the same element possess different nuclear properties. That is, some isotopes are stable, whereas others are unstable or radioactive.

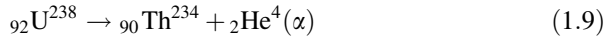
Radioactive isotopes undergo spontaneous nuclear change (i.e. transformation) at a definite rate in the direction of increasing stability of the element. During this transformation the unstable nucleus emits characteristic particles (i.e. high velocity particles or radiation) and is thereby transformed into a different nucleus which may or may not also be a radioactive element. Isotopes which owe their instability to

their high mass numbers emit either positively charged *alpha* (α) particles or negatively charged *beta* (β) particles.

- (a) Alpha (α) particles are identical with helium nuclei (${}_2\text{He}^4$) and consist of two protons and two neutrons. The product (or daughter) nucleus of alpha decay has two protons and two neutrons less than the parent nucleus, so that its mass number is four units less:



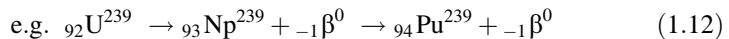
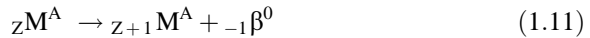
In other words, it produces an element in the Periodic Table (Fig. 1.1) two places to the left of the parent isotope. For example, α disintegration of ${}_{92}\text{U}^{238}$ results in its transformation into ${}_{90}\text{Th}^{234}$:



- (b) Beta (β) particles are identical to ordinary electrons. The nucleus itself does not contain electrons, and in radioactive beta decay the electron arises from the spontaneous conversion of a neutron into a proton and an electron:



The additional neutral particle, with essentially zero mass, called a *neutrino*, carries out some of the energy liberated in the radioactive transformation. In beta decay the daughter nucleus has one neutron less and one proton more than its parent, but the mass number is unchanged; i.e. this produces an element in the Periodic Table (Fig. 1.1) one place to the right of the parent element:



A neutron is replaced in the nucleus by a proton, so that the neutron/proton ratio decreases, the daughter nucleus will be more stable than its parent, not necessarily completely stable.

- (c) In many cases, although not always, radioactive decay is associated with the emission of gamma (γ) rays, in addition to an alpha (α) or beta (β) particles. Gamma (γ) rays are penetrating electromagnetic radiations of high energy, essentially identical with X rays. In fact, the only difference between γ rays and X rays is that the former originate from an atomic nucleus; whereas the later are produced by processes outside the nucleus.

γ rays occur in a radioactive change when the daughter nucleus is formed in what is called an excited state, i.e. a state in which it has a higher internal energy than the normal (or ground) state of that nucleus. The excess energy is then released almost instantaneously as γ radiation. Such an excited nucleus is known as an *isomer of the unexcited nucleus*.

1.5 Rate of Radioactive Decay

The rate of radioactive decay is a value characteristic of a given isotope and independent of the physical and chemical state of the element, at least under the conditions of temperature and pressure. In a given specimen, the rate of radioactive decay at any instant is always directly proportional to the number of radioactive atoms of the isotope under consideration present at that time. Thus, if N is the number of the particular radioactive atoms (or nuclei) present at any time t , the decay rate is given by:

$$(dN/dt) = -\lambda N \quad (1.13)$$

where λ is the radioactive decay (or disintegration) constant of the radioactive species, a measure of its decay probability. Minus sign indicates a decrease in the number of the particular radioactive atoms (or nuclei) i.e. N . This Eq. (1.13) permits a determination of N at a given time t , assuming that there were N_0 parent nuclei at the initial time t_0 . By integrate Eq. (1.13):

$$N = N_0 e^{-\lambda t} \quad (1.14)$$

The rate of radioactive disintegration is conveniently expressed by means of a so-called *half-life period* ($t_{1/2}$). It is defined as the time required for the number of radioactive nuclei of a given kind to decay to half its initial value. Assuming $N = 0.5N_0$ and applying to Eq. (1.14):

$$t_{1/2} = (0.6931/\lambda) \quad (1.15)$$

The reciprocal of the decay constant, represented by t_m , is known as *mean life* (or *average life*) of the radioactive species; thus,

$$t_m = 1/\lambda \quad (1.16)$$

The half-life is thus inversely proportional to the decay constant or by Eq. (1.15), directly proportional to the mean life, i.e.

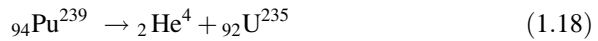
$$t_{1/2} = 0.6931 t_m \quad (1.17)$$

Some of the data for nuclides that are of direct or indirect interest as nuclear fuels are given in Table 1.1. The long half-life is important since it means that there are

Table 1.1 Radioactive characteristics of nuclear fuel isotopes

Nuclide	Radiation	Half-life, years
Th ²³²	α	1.39×10^{10}
U ²³³	α	1.62×10^5
U ²³⁵	α	7.13×10^8
U ²³⁸	α	4.51×10^9
Pu ²³⁹	α	2.44×10^4

no appreciable losses in storage over many hundreds of years. It is of interest that, when the fuel species with the shortest half-life, namely Pu²³⁹, decays its daughter is U²³⁵ having a much longer half-life.



Since the uranium (U²³⁵) is also a nuclear fuel, there is no appreciable loss in usefulness of the material as a source of energy.

Example 1.2 If $(dN/dt) = -\lambda N$, then prove that: $N = N_0 e^{-\lambda t}$

Solution:

$$(dN/dt) = -\lambda N$$

$$\text{By integrating } \int_{N_0}^N (dN/dt) = - \int_0^t \lambda N$$

$$\text{Or } \int_{N_0}^N (dN/N) = -\lambda \int_0^t dt \quad (\text{since } \lambda \text{ is constant})$$

$$\text{Or } (\ln N - \ln N_0) = -\lambda t \quad \text{or } \ln(N/N_0) = -\lambda t$$

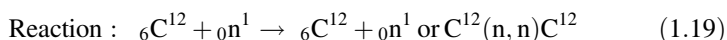
Hence, $N = N_0 e^{-\lambda t}$ **Prove**

1.6 Neutron Reaction

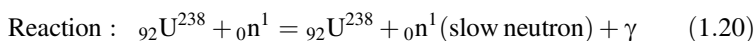
In addition to the spontaneous nuclear reactions due to radioactivity, in which one nucleus is changed into another as the result of a particle, there are many nuclear reactions which can be brought about artificially, resulting from the absorption of one particle or another. Among such reactions, those in which a neutron is absorbed are of special interest. Neutrons are normally bound in atomic nuclei, but it is possible to obtain these in the free state. Such free neutrons can interact in various ways with nuclei.

There are three types of neutron-nuclear interactions of importance in the operation of nuclear reactors, namely: (1) scattering; (2) capture; and (3) fission.

- (1) *Scattering*: The nucleus absorbs the neutron to form a compound nucleus in an excited state of higher internal energy. This compound nucleus rapidly expels a neutron with a lower kinetic energy than the absorbed neutron, the excess energy remaining on the residual nucleus.
- (a) A compound nucleus may emit a particle identical with the one absorbed by the nucleus, the total kinetic energy of the struck nucleus and the bombarding particle remaining unchanged. Such a process is referred to as *elastic scattering*. This kind of reaction neither releases nor absorbs energy, and its only result is a redistribution of the kinetic energy of the collision particles.



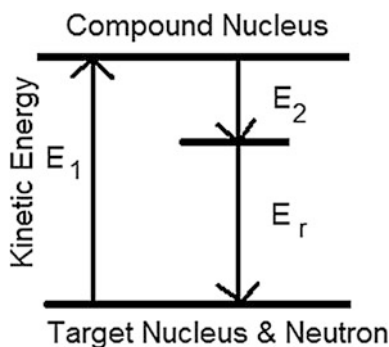
- (b) It may happen that the incident particle and the ejected particle are identical, but the total kinetic energy of the colliding particles decreases after the collision. The energy difference is emitted by the compound nucleus as a γ radiation. Such a process is called *inelastic scattering*.



Let E_1 is the total kinetic energy of the neutron and target nucleus before collision, and E_2 is the kinetic energy after collision; if E_γ is the energy emitted as γ radiation, then $E_1 = E_2 + E_\gamma$ (as shown in Fig. 1.2).

- (2) *Capture*: The bombarding particle may be trapped in the nucleus. In this case the excitation energy of the compound nucleus is carried away by the γ radiation emitted after absorption of the particle. Such a process is called *capture*. The capture of a neutron by a nucleus followed by the emission of γ radiation.

Fig. 1.2 Kinetic energy of the neutron and target nucleus before and after collision



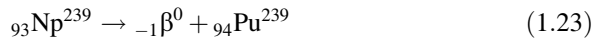
In this reaction the neutron is taken up by the reacting (or target) nucleus in a high energy state. Within a small fraction of a second, the compound nucleus emits the excess energy as radiation, leaving a nucleus differing by one neutron from the target nucleus:



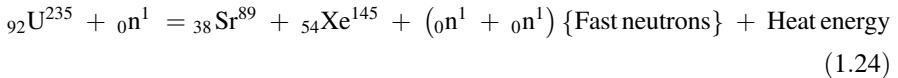
The resulting nucleus, U-239, is radioactive and decays with the emission of a negative beta particle (${}_{-1}\beta^0$). Thus:



The product, Np-239 being an isotope of an element of atomic number 93, called neptunium (Np), which does not normally exist on earth. Np-239 is also beta active and decays fairly rapidly.



(3) *Fission*: When a compound nucleus attains such a state of excitation that it splits into two parts of lighter masses. This process is called *fission*. When certain nuclei of higher atomic number and mass number capture neutrons, the resulting excited compound nucleus, instead of emitting its excess energy as γ radiation, splits into two lighter nuclei having masses very different from that of the original heavy nucleus.



When first liberated, free neutrons usually possess high kinetic energies, in the million electron volt range, and so they are called *fast neutrons*. The fission reaction is the basic to the operation of nuclear reactors. Fission occurs only with nuclei of high atomic (and mass) number, and the large value of Z^2 , and hence the repulsive force within the nucleus, is an important contributory factor. When fission occurs, the excited compound nucleus formed after absorption of a neutron breaks up into two lighter nuclei, called *fission fragments*.

The important of fission, from the standpoint of the utilization of nuclear energy, lies in two facts: (a) the process is associated with the release of a large amount of energy per unit mass of nuclear fuel; and (b) the fission reaction, which is initiated by neutron, is accompanied by the liberation of neutrons.